

Warm up

Find the trig ratio for the following:

1. $\sin \frac{\pi}{3}$

2. $\cos \frac{\pi}{4}$

3. $\csc \frac{\pi}{6}$

4. $\tan 30^\circ$

5. $\sec 45^\circ$

6. $\cot 45^\circ$

Find θ in degrees.

7. $\sin \theta = \frac{1}{\sqrt{2}}$

 $45^\circ, 135^\circ$

8. $\csc \theta = \frac{2}{\sqrt{3}}$

 60°

9. $\cot \theta = \sqrt{3}$

 30°

10. $\cos \theta = \frac{1}{2}$

 $60^\circ, 300^\circ$

Workbook Answers

- | | |
|--------------------|----------------------|
| 1. 7.73 rad/min | 2. 12.99 rad/sec |
| 3. 1441.94 rev/min | 4a. 14.29 m/sec |
| | 4b. 211.6 cm/sec |
| 5a. 5.28 cm/sec | 6. 104.72 rad/sec |
| 5b. 8.73 cm/sec | |
| 7. 17.45 ft/sec | 8. fastest - outside |
| 9. 17222.54 mph | 10. 728.29 rev/min |

4.4 Trig Functions of any angle Day 1

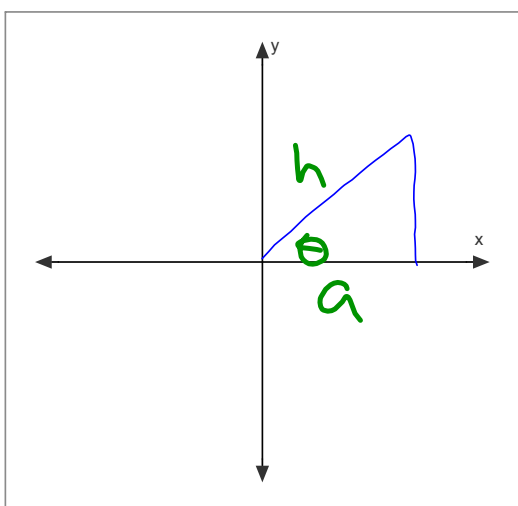
trig ratios for angles > 90 or $\frac{\pi}{2}$

ASTC

Quadrant values

What quadrant am I in?

So far we have talked only about trig ratios of acute angles. What if the angle I want to evaluate is obtuse?



Remember that on the unit circle

$$(x, y) = (\cos \theta, \sin \theta)$$

$$= (\text{adj side}, \text{opp side})$$

$$\cos 60^\circ = \frac{1}{2}$$

Example: Let $(5, -12)$ be a point on the terminal side of angle θ , find $\sin \theta$, $\cos \theta$, $\tan \theta$

Step 1: Draw a triangle

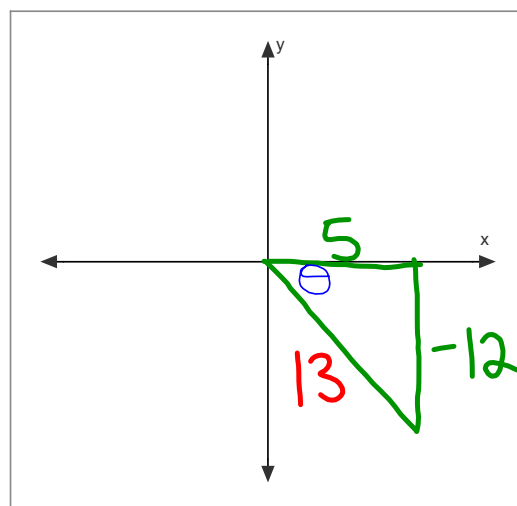
Step 2: Find the third side

Step 3: Find the ratios

$$\sin \theta = -\frac{12}{13}$$

$$\cos \theta = \frac{5}{13}$$

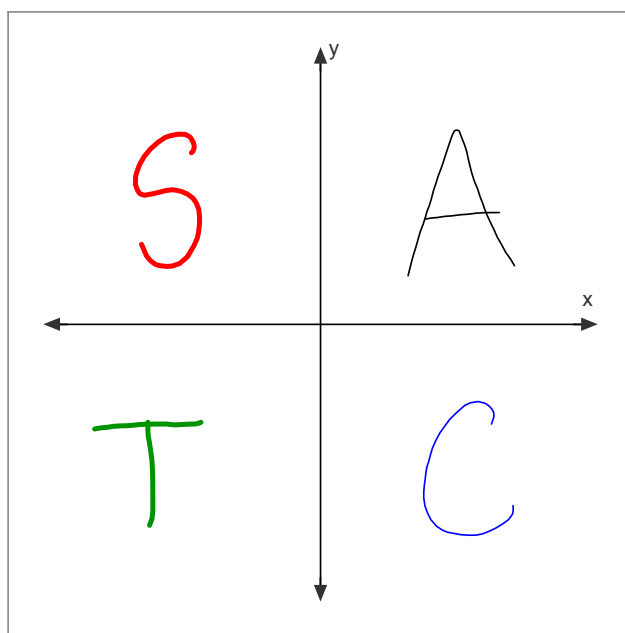
$$\tan \theta = -\frac{12}{5}$$



ASTC

$$(x, y) = (\cos \theta, \sin \theta)$$
$$= (\text{adj side}, \text{opp side})$$

$$\frac{\sin \theta}{\cos \theta} = \tan \theta$$



ALL trig ratios are positive

SIN ratio is positive

TAN ratio is positive

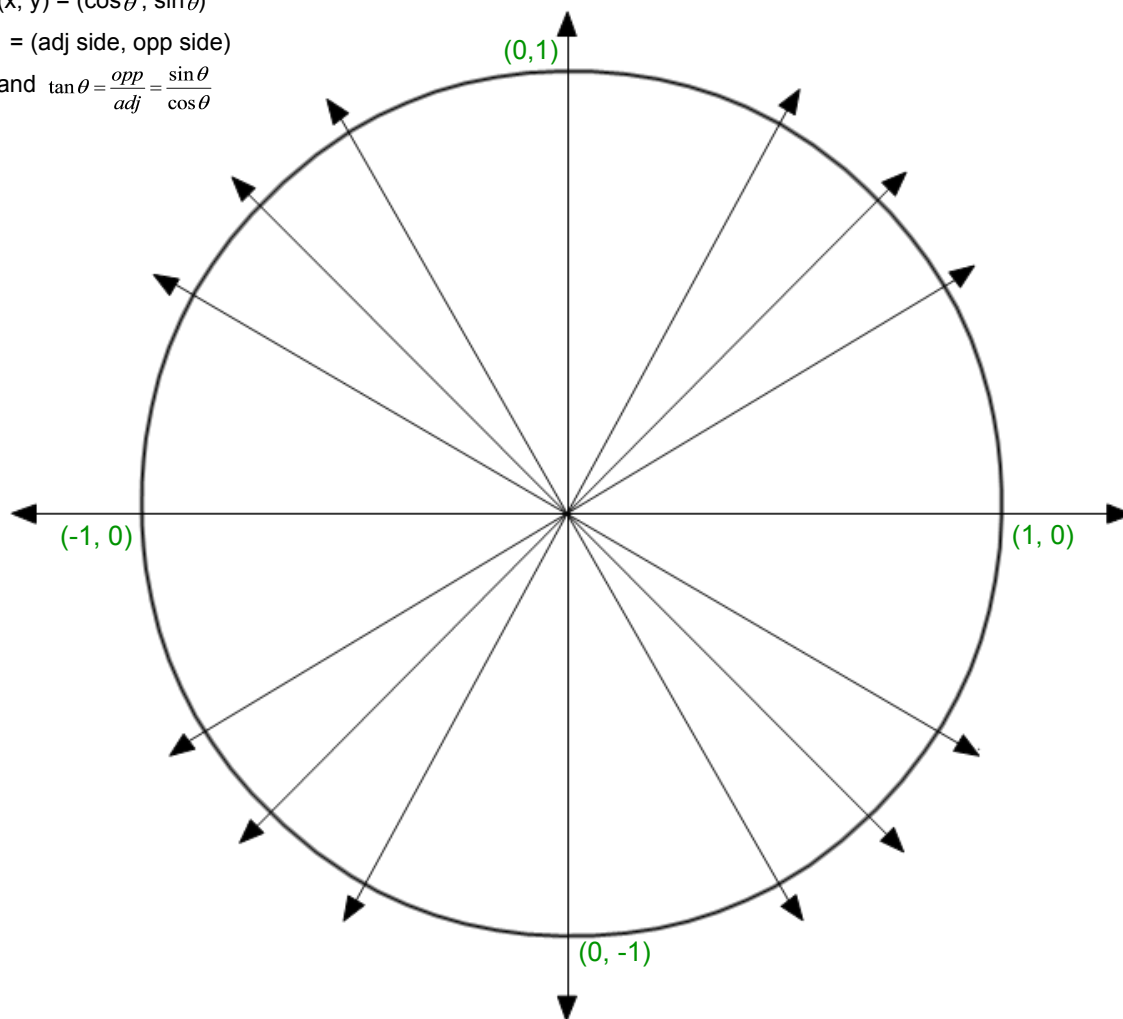
COS ratio is positive

Remember:

$$(x, y) = (\cos \theta, \sin \theta)$$

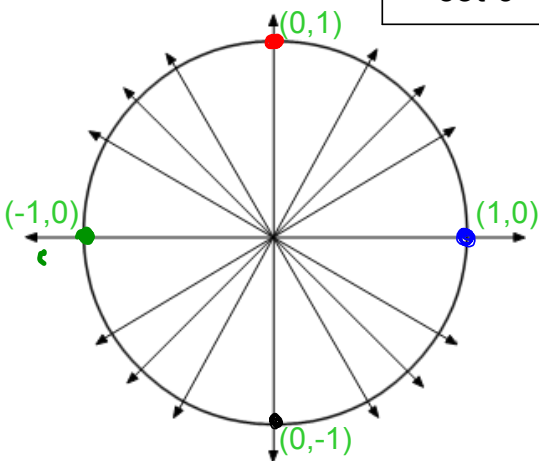
$$= (\text{adj side}, \text{opp side})$$

$$\text{and } \tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{\sin \theta}{\cos \theta}$$



$\sin 2\pi$
 $\csc 2\pi$

	0, 360 or 0, 2π	90 or $\pi/2$	180 or π	270 or $3\pi/2$
$\sin \theta$	$0/1 = 0$	$1/1 = 1$	$0/1 = 0$	$-1/1 = -1$
$\cos \theta$	$1/1 = 1$	$0/1 = 0$	$-1/1 = -1$	$0/1 = 0$
$\tan \theta$	$0/1 = 0$	$1/0 = \text{und}$	$0/-1 = 0$	$-1/0 = \text{und}$
$\csc \theta$	$1/0 = \text{und}$	$1/1 = 1$	$1/0 = \text{und}$	$1/-1 = -1$
$\sec \theta$	$1/1 = 1$	$1/0 = \text{und}$	$1/-1 = -1$	$1/0 = \text{und}$
$\cot \theta$	$1/0 = \text{und}$	$0/1 = 0$	$-1/0 = \text{und}$	$0/-1 = 0$

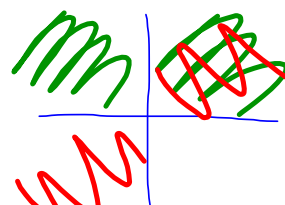


$$\sin \pi = \frac{y}{r} = \frac{0}{1}$$

$$\csc \pi = \frac{r}{y} = \frac{1}{0}$$

What quadrant am I in??

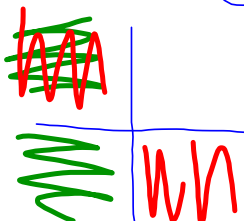
$\sin \theta > 0$ $\tan \theta > 0$ Q1



$\cos \theta < 0$ $\sin \theta < 0$ Q3

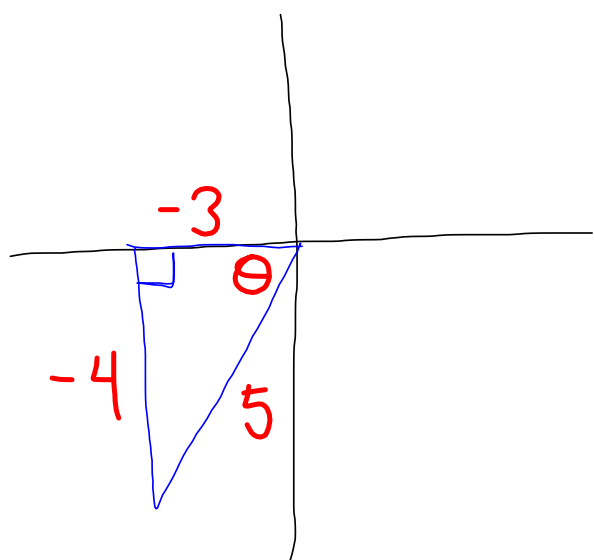
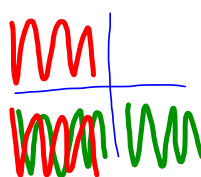


$\sec \theta < 0$ $\cot \theta < 0$ Q2



find the remaining 5 trig ratios (values) given:

$$\sin \theta = -\frac{4}{5}, \quad \cos \theta < 0$$



$$\cos \theta = -\frac{3}{5}$$

$$\tan \theta = \frac{4}{3}$$

$$\csc \theta = \frac{5}{-4}$$

$$\sec \theta = \frac{5}{-3} \quad \cot \theta = \frac{3}{4}$$

Homework

p 294

due tues.

1-21 odd, 29-36 all

Optional Quiz Review

p 265

1-19 odd, 23-73 odd, 77, 78, 96-100

p 284

1-4, 9-33, 57-66, 78, 79

