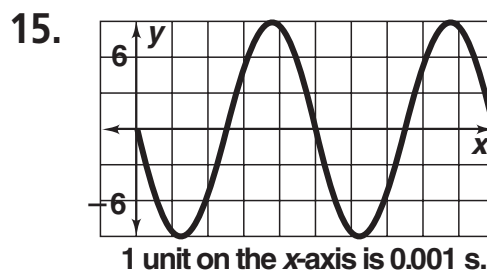
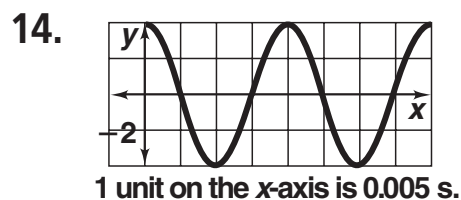


## Answers for Lesson 13-1 Exercises

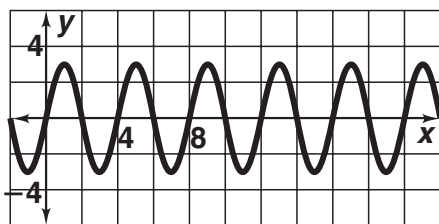
1.  $x = -2$  to  $x = 3$ ,  $x = 2$  to  $x = 7$ ; 5
2.  $x = 0$  to  $x = 4$ ,  $x = 5$  to  $x = 9$ ; 4
3.  $x = 0$  to  $x = 4$ ,  $x = 2$  to  $x = 6$ ; 4
4. not periodic
5. periodic; 12
6. not periodic
7. not periodic
8. periodic; 8
9. periodic; 7
10. 4
11. 3
12. 1
13. 2



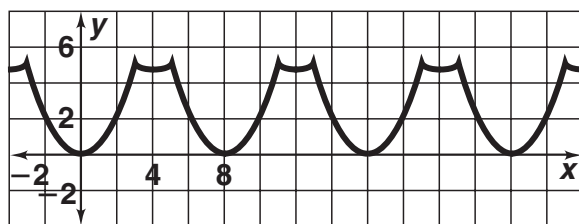
16. a.  $y$   
b.  $x$
17. Answers may vary. Sample: Yes; average monthly temperatures for three years should be cyclical due to the variation of the seasons.
18. Answers may vary. Sample: No; population usually increases or decreases but is not cyclical.
19. Answers may vary. Sample: Yes; traffic that passes through an intersection should be at the same levels for the same times of day for two consecutive work days.
20. 60 beats per min
21. a. 1 s  
b. 1.5 mV
22. Check students' work.

## Answers for Lesson 13-1 Exercises (cont.)

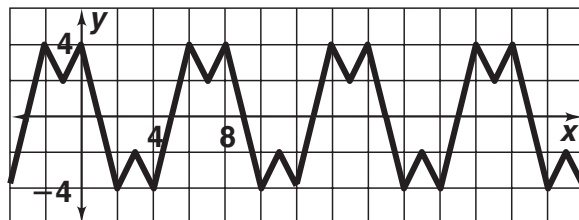
23. 3, -3, 4;



24. 5, 0, 8;



25. 4, -4, 8;



26. 1 yr

27. 2 weeks

28. 3 months

29. 1 hour

30. 1 day

31. 2, 2, 2

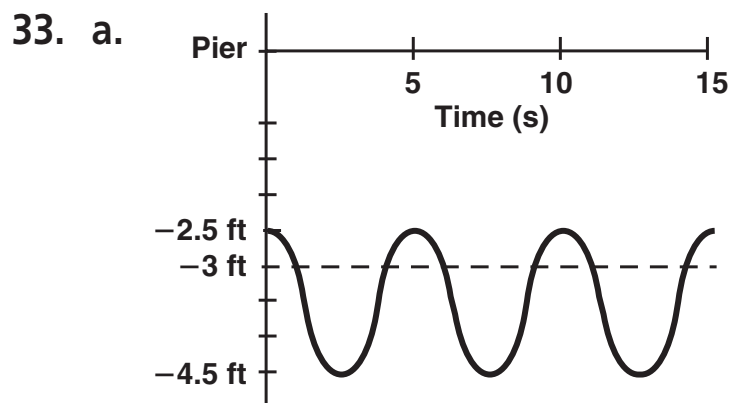
32. a. 67

b. 70

c. 70

d. 67

## Answers for Lesson 13-1 Exercises (cont.)



- b. 5 s, 1 ft  
 c. Answers may vary. Sample: about  $1\frac{1}{3}$ s

34. a. 24.22 days  
 b. 0.78 day  
 c. 0.22 day  
 d. Answers may vary. Sample: The calendar year is meant to predict events in the solar year. Keeping the difference between the two minimal is necessary for the calendar year to be useful.

## Answers for Lesson 13-2 Exercises

1.  $-315^\circ$

2.  $-135^\circ$

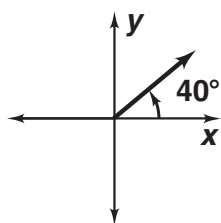
3.  $240^\circ$

4.  $115^\circ$

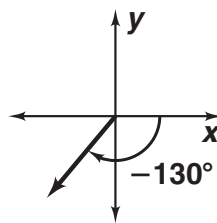
5.  $-110^\circ$

6.  $-340^\circ$

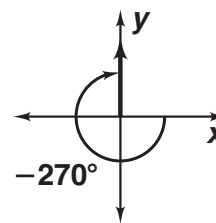
7.



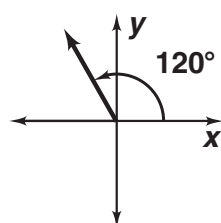
8.



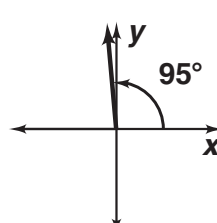
9.



10.



11.



12.  $25^\circ$

13.  $215^\circ$

14.  $315^\circ$

15.  $4^\circ$

16.  $140^\circ$

17.  $150^\circ$

18.  $55^\circ$

19.  $180^\circ$

20. Answers may vary. Sample:  $-135^\circ, 585^\circ$

21.  $\frac{1}{2}, -\frac{\sqrt{3}}{2}; 0.50, -0.87$

22.  $-\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}; -0.71, -0.71$

23.  $\frac{\sqrt{3}}{2}, -\frac{1}{2}; 0.87, -0.50$

24.  $-\frac{1}{2}, \frac{\sqrt{3}}{2}; -0.50, 0.87$

25.  $\frac{\sqrt{3}}{2}, \frac{1}{2}; 0.87, 0.50$

26.  $\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}; 0.71, -0.71$

27.  $\frac{\sqrt{3}}{2}, -\frac{1}{2}; 0.87, -0.50$

28.  $-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}; -0.71, 0.71$

29. 1.00, 0.00

30. 0.85, 0.53

31. 0.71,  $-0.71$

32.  $-0.87, 0.50$

33.  $-0.09, -1.00$

34. 0.98,  $-0.17$

35.  $-0.90, 0.44$

36. 0.00, 1.00

**37–44. Answers may vary. Samples:**

37.  $405^\circ, -315^\circ$

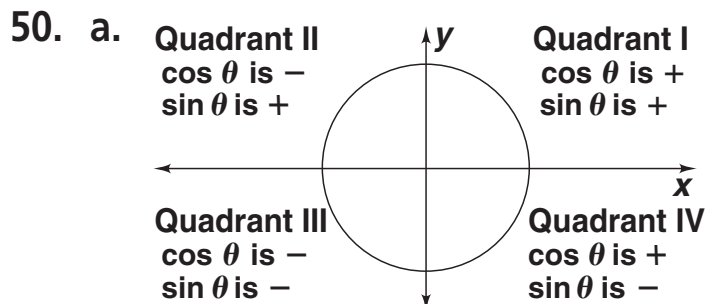
38.  $235^\circ, -485^\circ$

39.  $45^\circ, -315^\circ$

40.  $40^\circ, -320^\circ$

## Answers for Lesson 13-2 Exercises (cont.)

41.  $275^\circ, -445^\circ$       42.  $295^\circ, -65^\circ$       43.  $573^\circ, -147^\circ$   
 44.  $303^\circ, -417^\circ$       45. II      46. III  
 47. negative  $x$ -axis      48. IV      49. positive  $x$ -axis



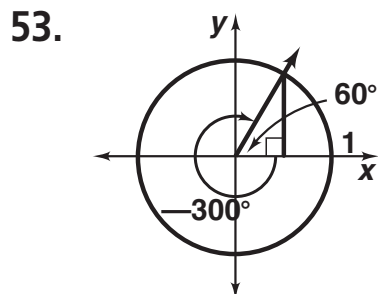
b. II

c. If the terminal side of an angle is in Quadrants I or II, then the sine of the angle is positive; otherwise it is not. If the terminal side of an angle is in Quadrants I or IV, then the cosine of the angle is positive; otherwise it is not.

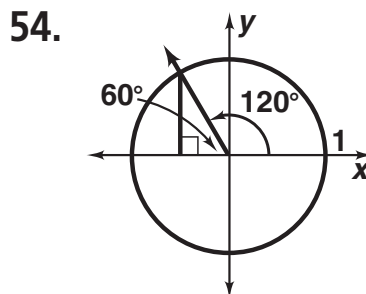
51. a. 0.77, 0.77, 0.77

b. The cosines of the three angles are equal because the angles are coterminal.

52. The  $x$ -coordinate of the point on the ray defined by angle  $\theta$  is equal to  $\cos \theta$ ; similarly for the  $y$ -coordinate and  $\sin \theta$ . The terminal sides of the angles  $0^\circ$ ,  $180^\circ$ , and  $360^\circ$  lie on the  $x$ -axis, and thus their sines are all 0 and their cosines are  $\pm 1$ . The angles  $90^\circ$  and  $270^\circ$  lie on the  $y$ -axis, so their cosines are 0 and their sines are 1 and  $-1$  respectively.

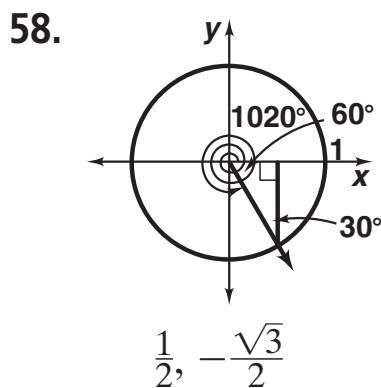
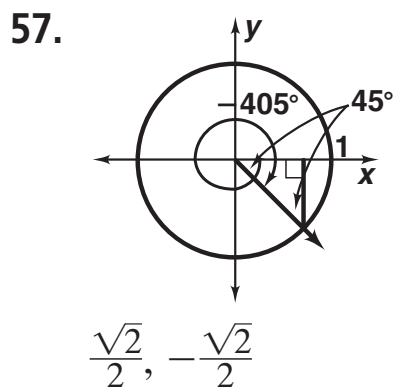
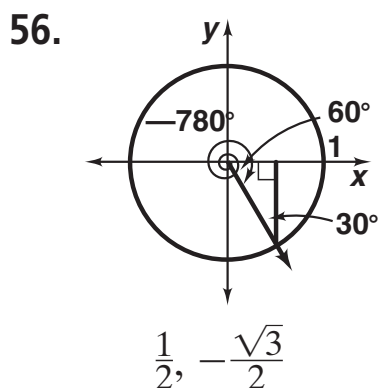
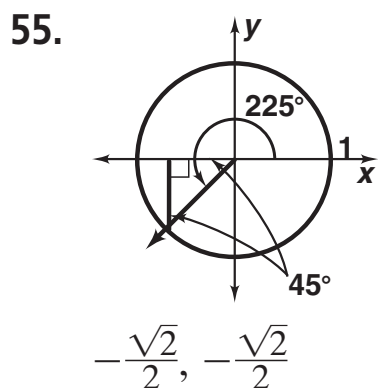


$$\frac{1}{2}, \frac{\sqrt{3}}{2}$$



$$-\frac{1}{2}, \frac{\sqrt{3}}{2}$$

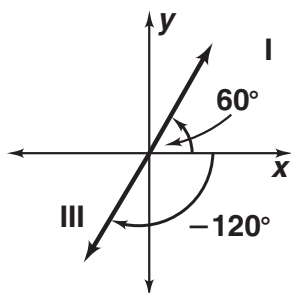
## Answers for Lesson 13-2 Exercises (cont.)



59.  $\left(-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$

60. Answers may vary. Sample:  $30^\circ, 150^\circ, -210^\circ, 390^\circ$

61. No; yes; if the  $\sin \theta$  and  $\cos \theta$  are both negative,  $\theta$  is in Quadrant III.  $-120^\circ$  is in Quadrant III.

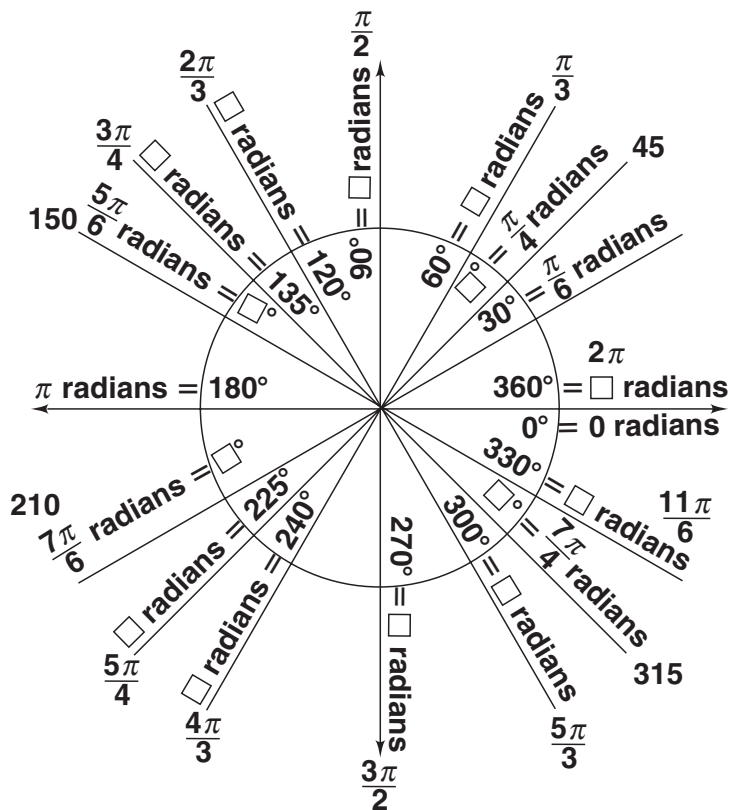


62. a. Check students' work.

b.  $-20^\circ$

## Answers for Lesson 13-3 Exercises

1.  $-\frac{5\pi}{3}, -5.24$
2.  $\frac{5\pi}{6}, 2.62$
3.  $-\frac{\pi}{2}, -1.57$
4.  $-\frac{\pi}{3}, -1.05$
5.  $\frac{8\pi}{9}, 2.79$
6.  $\frac{\pi}{9}, 0.35$
7.  $540^\circ$
8.  $198^\circ$
9.  $-120^\circ$
10.  $-172^\circ$
11.  $90^\circ$
12.  $270^\circ$
- 13.



14.  $\frac{\sqrt{3}}{2}, \frac{1}{2}$
15.  $\frac{1}{2}, \frac{\sqrt{3}}{2}$
16.  $0, 1$
17.  $-\frac{1}{2}, \frac{\sqrt{3}}{2}$
18.  $-\frac{\sqrt{3}}{2}, \frac{1}{2}$
19.  $0, -1$
20. 3.1 cm
21. 10.5 m
22. 51.8 ft
23. 25.1 in.
24. 4.7 m
25. 43.2 cm
26.  $\approx 107$  in.
27.  $\approx 32$  ft

## Answers for Lesson 13-3 Exercises

28. a.  $\approx 11,048$  km  
 b.  $\approx 33,144$  km  
 c.  $\approx 27,620$  km  
 d.  $\approx 276,198$  km  
 e. 18.1 h

29.  $\approx 42.2$  in.

30. a.  $15^\circ, \frac{\pi}{12}$  radians  
 b.  $\approx 1036.7$  mi  
 c.  $\approx 413.6$  mi

31. III

32. II

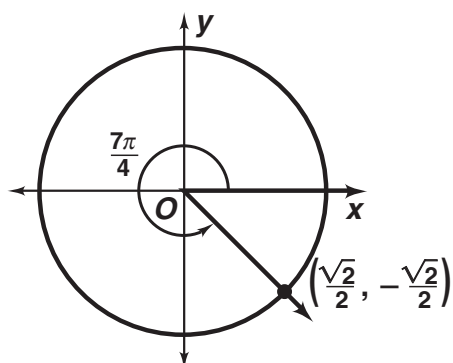
33. positive  $y$ -axis

34. II

35. negative  $x$ -axis

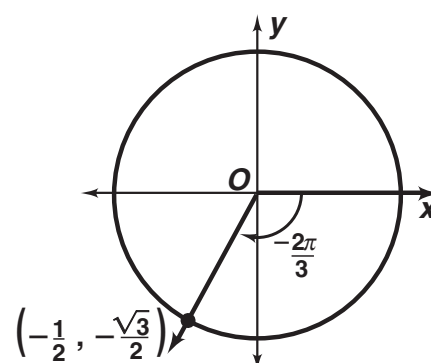
36. III

37.



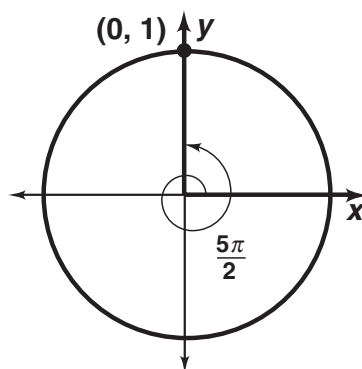
0.71, -0.71

38.



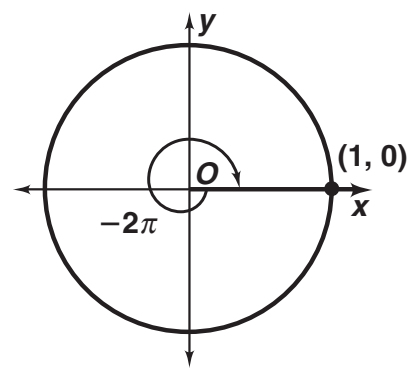
-0.50, -0.87

39.



0.00, 1.00

40.

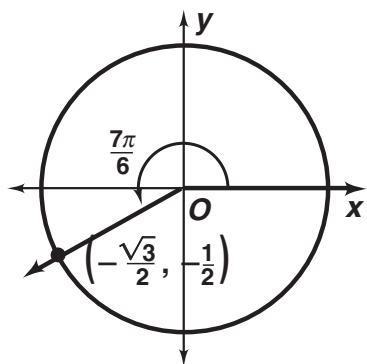


1.00, 0.00



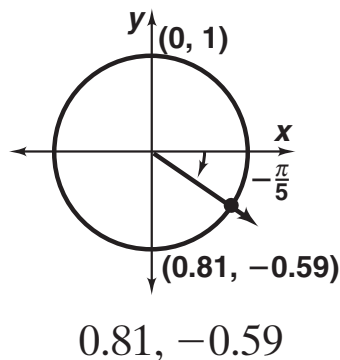
## Answers for Lesson 13-3 Exercises

41.

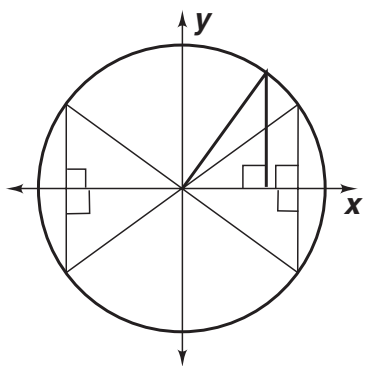


$-0.87, -0.50$

42.



43. a-b.



c. All five triangles are congruent by SSS. All have a hypotenuse of 1 unit, a long leg of about 0.81 unit, and a short leg of 0.59 unit.

$$\cos \frac{\pi}{5} \approx 0.81, \sin \frac{\pi}{5} \approx 0.59;$$

$$\sin \frac{3\pi}{10} \approx 0.81, \cos \frac{3\pi}{10} \approx 0.59;$$

$$\cos \frac{4\pi}{5} \approx -0.81, \sin \frac{4\pi}{5} \approx 0.59;$$

$$\cos \frac{6\pi}{5} \approx -0.81, \sin \frac{6\pi}{5} \approx -0.59;$$

$$\cos \frac{9\pi}{5} \approx 0.81, \sin \frac{9\pi}{5} \approx -0.59$$

44. Check students' work.

45.  $\approx 11$  radians

46. The student forgot to include parentheses around  $2*\pi$ .

47.  $\approx 798$  ft;  $55^\circ$ ,  $-665^\circ$

48.  $\approx 23.6$  in.; Sample:  $-\frac{7\pi}{6}$ ,  $\frac{17\pi}{6}$

## Answers for Lesson 13-3 Exercises

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49. If two angles measured in radians are coterminal, the difference of their measures will be evenly divisible by  $2\pi$ .

50.  $\approx 6.3$  cm

51.  $\approx 4008.7$  mi

52.  $-\frac{3\pi}{2}$  radians

53.  $-\frac{11\pi}{3}$  radians

54.  $\frac{4\pi}{3}$  radians

55.  $\frac{35\pi}{6}$  radians

56. 
$$\frac{\theta}{2\pi} = \frac{s}{2\pi r}$$
$$\frac{\theta}{2\pi} \cdot 2\pi r = \frac{s}{2\pi r} \cdot 2\pi r$$
$$\theta r = s$$
$$s = r\theta$$

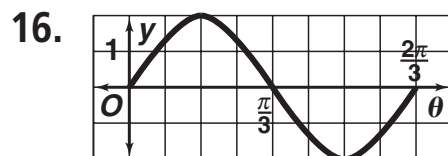
57. a. 0.5017962; 0.4999646; the first four terms

b.  $1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \frac{x^8}{8!} - \dots$

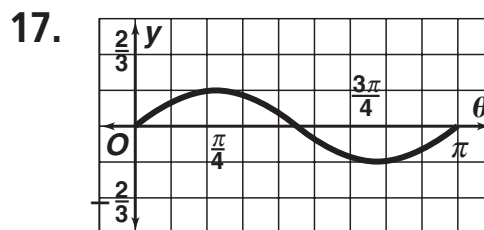
c.  $\approx 0.951$ ;  $18^\circ$

## Answers for Lesson 13-4 Exercises

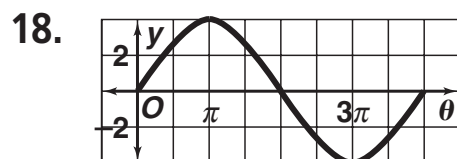
1.  $\frac{1}{2}$       2.  $\approx 0.7$       3.  $\approx 0.9$   
 4. 0      5.  $\approx -0.9$       6.  $\approx -0.9$   
 7. 1      8.  $\approx 0.1$       9.  $\approx -0.8$   
 10.  $\approx -1$       11. -1      12.  $\approx -0.7$   
 13. 3; 2,  $\frac{2\pi}{3}$       14.  $\frac{1}{2}$ ; 1,  $4\pi$       15. 2; 3,  $\pi$



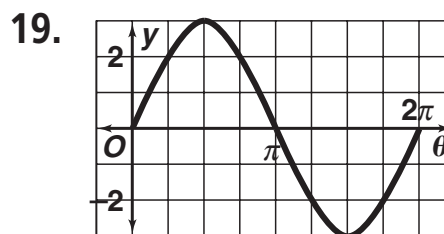
$$y = 2 \sin 3\theta$$



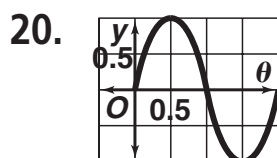
$$y = \frac{1}{3} \sin 2\theta$$



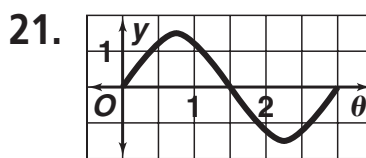
$$y = 4 \sin \frac{1}{2}\theta$$



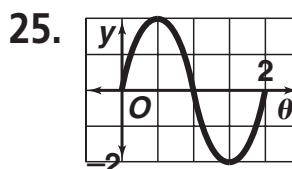
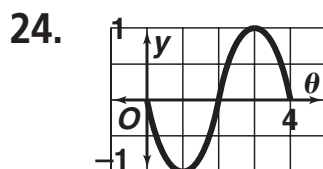
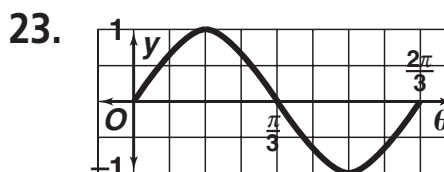
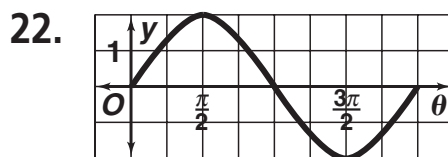
$$y = 3 \sin \theta$$



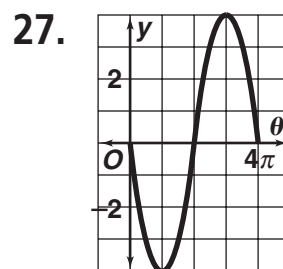
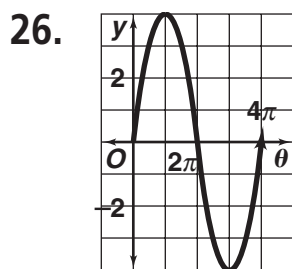
$$y = \sin \pi\theta$$



$$y = 1.5 \sin \frac{2\pi}{3}\theta$$



## Answers for Lesson 13-4 Exercises (cont.)



28.  $2\pi; y = 2 \sin \theta$

29.  $2\pi; y = -3 \sin \theta$

30.  $\pi; y = \frac{5}{2} \sin 2\theta$

31.  $\frac{\pi}{3}; y = \frac{1}{2} \sin 6\theta$

32.  $\pi; y = -\sin 2\theta$

33.  $4; y = 3 \sin \frac{\pi}{2}\theta$

34.  $1; 1, 2\pi$

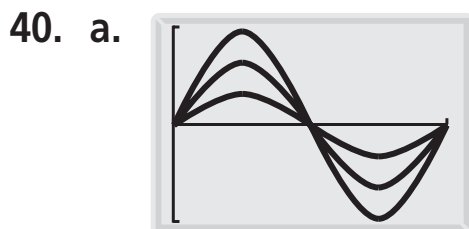
35.  $5; 1, \frac{2\pi}{5}$

36.  $\pi; 1, 2$

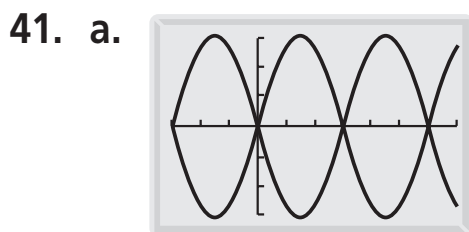
37.  $1; 3, 2\pi$

38.  $1; 5, 2\pi$

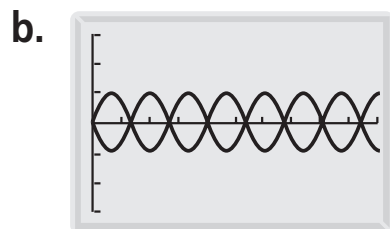
39.  $2\pi; 5, 1$



b. As  $a$  increases, the amplitude of the graph increases.



They are reflections of each other in the  $x$ -axis.



They are reflections of each other in the  $x$ -axis.

c. When either  $a$  or  $b$  is replaced by its opposite, the graph is a reflection of the original graph in the  $x$ -axis.

## Answers for Lesson 13-4 Exercises (cont.)

42. a.  $\pi$

b. 4

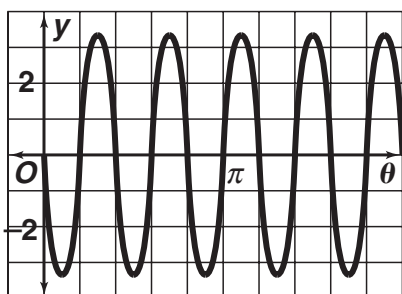
43. a.  $\frac{1}{440}$

b. 0.001

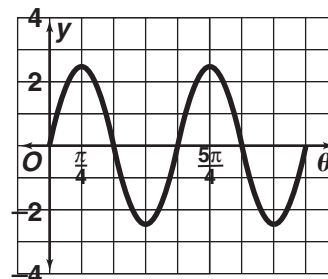
c.  $880\pi$

44. •  $|a|$  is the amplitude of the function.  
 •  $b$  is the number of cycles in the interval  $0^\circ$  to  $360^\circ$ .  
 •  $\frac{360^\circ}{b}$  is the period of the function. The properties relating to number of cycles and period are affected.

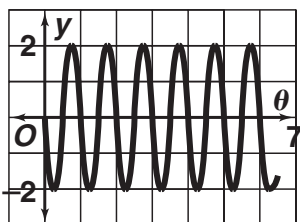
45.  $\frac{2\pi}{5}, 3.5$



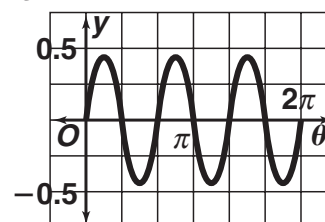
46.  $\pi, \frac{5}{2}$



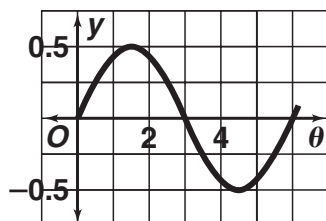
47. 1, 2



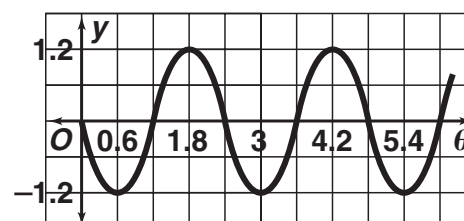
48.  $\frac{2\pi}{3}, 0.4$



49. 6, 0.5



50.  $\frac{12}{5}, 1.2$



51. Check students' work.

## Answers for Lesson 13-4 Exercises (cont.)

52. a.  $4, 2\pi$

b.  $y = 4 \sin \theta$

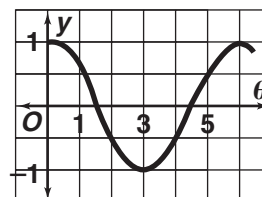
c. coil B

53.  $y = \sin 60\pi\theta$

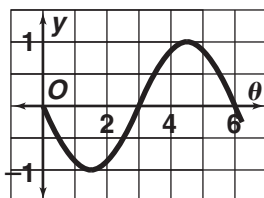
54.  $y = \sin 30\pi\theta$

55.  $y = \sin 240,000\pi\theta$

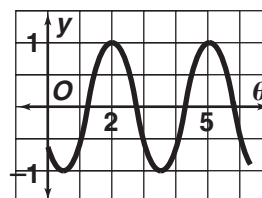
56.  $2\pi, 1$



57.  $2\pi, 1$



58.  $\pi, 1$



59. a. days from spring equinox, hours of sunlight

b.  $\frac{23}{12}$  h, about 365 days

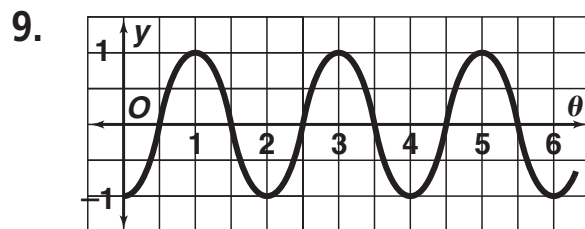
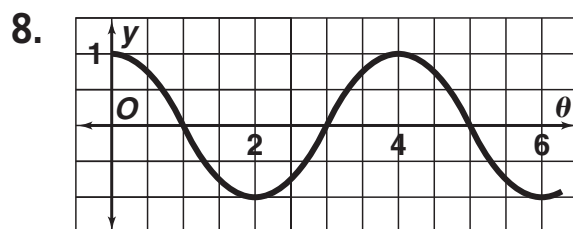
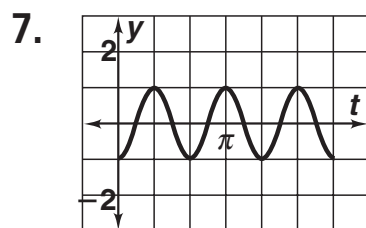
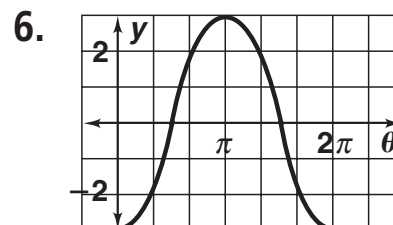
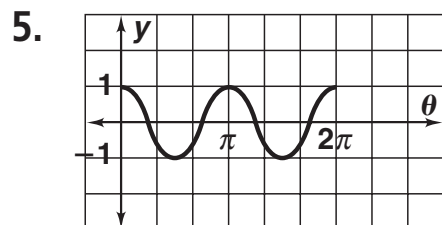
c.  $y = \frac{23}{12} \sin \frac{2\pi x}{365}$

d. 1.1 h

e. Check students' work.

## Answers for Lesson 13-5 Exercises

1.  $2\pi, 3$ ; max:  $0, 2\pi$ ; min:  $\pi$ ; zeros:  $\frac{\pi}{2}, \frac{3\pi}{2}$
2.  $\frac{2\pi}{3}, 1$ ; max:  $0, \frac{2\pi}{3}, \frac{4\pi}{3}, 2\pi$ ; min:  $\frac{\pi}{3}, \pi, \frac{5\pi}{3}$ ; zeros:  $\frac{\pi}{6}, \frac{\pi}{2}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{3\pi}{2}, \frac{11\pi}{6}$
3.  $\pi, 1$ ; max:  $0, \pi, 2\pi$ ; min:  $\frac{\pi}{2}, \frac{3\pi}{2}$ ; zeros:  $\frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$
4.  $2\pi, 2$ ; max:  $\pi$ ; min:  $0, 2\pi$ ; zeros:  $\frac{\pi}{2}, \frac{3\pi}{2}$



10.  $y = 2 \cos 2\theta$
11.  $y = \frac{\pi}{2} \cos \frac{2\pi}{3}\theta$
12.  $y = \pi \cos \pi\theta$
13.  $y = -3 \cos 2\theta$
14.  $y = 2 \cos \frac{\pi}{4}\theta$
15.  $y = 4 \cos \frac{2\pi}{3}\theta$
16. 0.52, 2.62, 3.67, 5.76
17. 1.98, 4.30
18. 0.55, 1.45, 2.55, 3.45, 4.55, 5.45

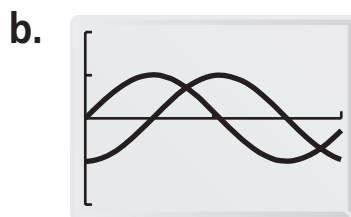
## Answers for Lesson 13-5 Exercises (cont.)

19. 2.52
20. 0.00
21. 0.86, 5.14
22.  $2\pi, -3 \leq y \leq 3, 3$
23.  $\pi, -1 \leq y \leq 1, 1$
24.  $4\pi, -2 \leq y \leq 2, 2$
25.  $4\pi, -\frac{1}{3} \leq y \leq \frac{1}{3}, \frac{1}{3}$
26.  $6\pi, -3 \leq y \leq 3, 3$
27.  $\frac{2\pi}{3}, -\frac{1}{2} \leq y \leq \frac{1}{2}, \frac{1}{2}$
28.  $\frac{4}{3}, -16 \leq y \leq 16, 16$
29. 2,  $-0.7 \leq y \leq 0.7, 0.7$
30. 0.64, 2.50
31. 1.83, 2.88, 4.97, 6.02
32. 0.50, 2.50, 4.50
33. a. 3.79, 5.64
- b. 10.07, 11.92; these values are the sums of the values from part (a) and  $2\pi$ .
34. a.
- b. Answers may vary. Sample: 0 s, 4 s, 8 s, 12 s
- c. 2 s; 2 s
35. a. 5.5 ft; 1.5 ft
- b. about 12 h 22 min
- c.  $y = 1.5 \cos \frac{2\pi t}{742}$
- d. 12:17 A.M.–7:49 A.M., 12:39 P.M.–8:11 P.M.



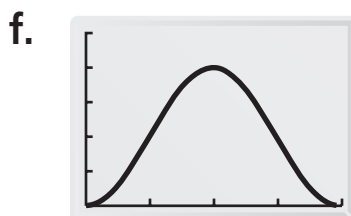
## Answers for Lesson 13-5 Exercises (cont.)

36. a. Answers may vary. Sample: sine; The sine function gives vertical position with respect to the center of the wheel.



Answers may vary. Sample: Going from left to right, the graph of  $Y2 = \sin\left(x - \frac{\pi}{2}\right)$  “trails” the graph of  $Y1 = \sin x$  by  $\frac{\pi}{2}$  units. If the “ride” for  $Y2$  would start  $\frac{\pi}{2}$  units of time sooner than the ride for  $Y1$ , the two graphs would be identical from the origin on out.

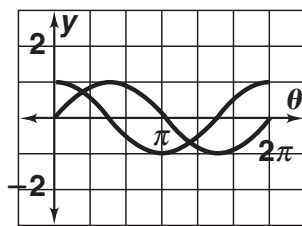
- c. 20 times as great  
 d. The center of the Ferris wheel is 20 ft higher at  $(0, 20)$   
 e.  $f(x) = 20 \sin\left(x - \frac{\pi}{2}\right) + 20$



- g. Allow for different values of 2 in  $f(x) = 20 \sin b\left(x - \frac{\pi}{2}\right) = 20$ . Model faster Ferris wheel speed by increasing the value of  $b$ . You can keep the starting point of the model at  $(0, 0)$  by letting  $b$  have value  $4n - 3$ ,  $n = 1, 2, \dots$   
 h. In parametric mode, let  $X_{1T} = T$ ,  $Y_{1T} = 20 \sin\left(T - \frac{\pi}{2}\right) + 20$  and adjust Tstep values.  
 i. Answers may vary. Sample: You can use the cosine function to model horizontal position with respect to the center of the wheel.

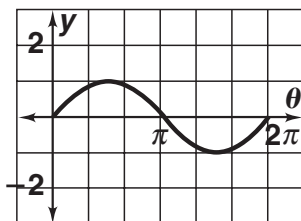
## Answers for Lesson 13-5 Exercises (cont.)

37. a.



shift of  $\frac{\pi}{2}$  units to the right

b.



They are the same.

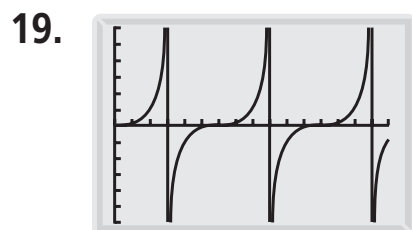
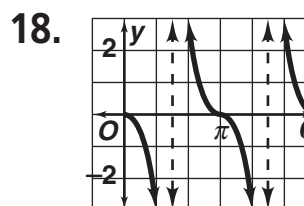
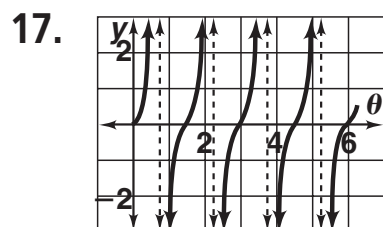
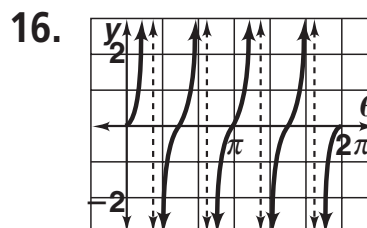
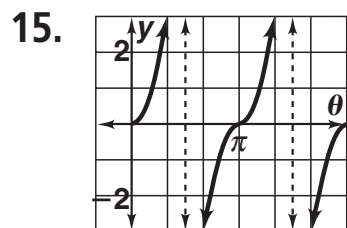
c. To write a sine function as a cosine function, replace  $\sin$  with  $\cos$  and replace  $\theta$  with  $\theta - \frac{\pi}{2}$ .

38.  $y = \cos \frac{\pi}{12}x$  or  $y = -\cos \frac{\pi}{12}x$

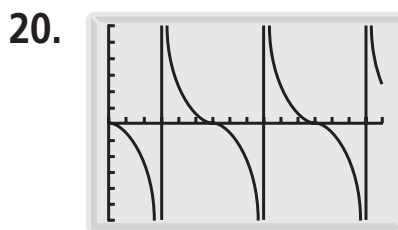
39. On the unit circle, the  $x$ -values of  $-\theta$  are equal to the  $x$ -values of  $\theta$ , so  $\cos(-\theta) = \cos \theta$ .  $-\cos \theta$  is the opposite of  $\cos \theta$ , so these graphs are reflections of each other over the  $x$ -axis.

## Answers for Lesson 13-6 Exercises

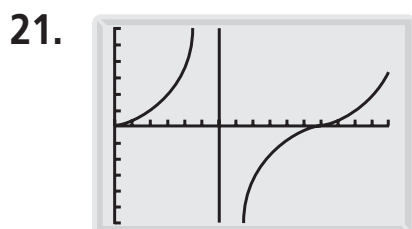
1. 0                      2. 0                      3. -1  
 4. undefined          5. 1                      6. 0  
 7. 1                      8. undefined          9.  $\pi$   
 10.  $\frac{\pi}{2}$                   11.  $\frac{\pi}{5}, \theta = -\frac{\pi}{10}, \frac{\pi}{10}$       12.  $\frac{2\pi}{3}, \theta = -\frac{\pi}{3}, \frac{\pi}{3}$   
 13.  $\frac{\pi}{4}, \theta = -\frac{\pi}{8}, \frac{\pi}{8}$       14.  $\frac{3\pi^2}{2}, \theta = -\frac{3\pi^2}{4}, \frac{3\pi^2}{4}$



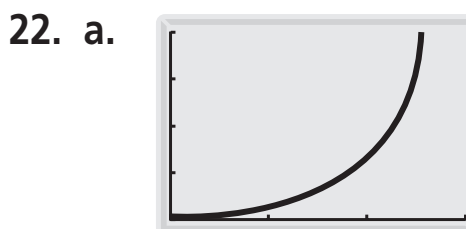
50, undefined, -50



-100, undefined, 100



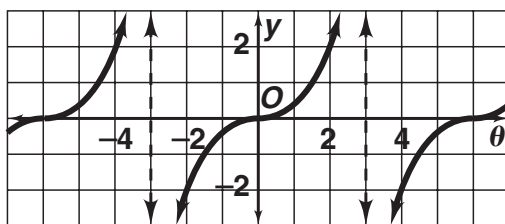
$\approx 51.8, 125, \approx 301.8$



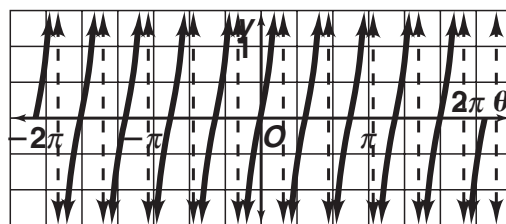
- b.  $\approx 14.3$  ft  
 c.  $\approx 20.2$  ft

## Answers for Lesson 13-6 Exercises (cont.)

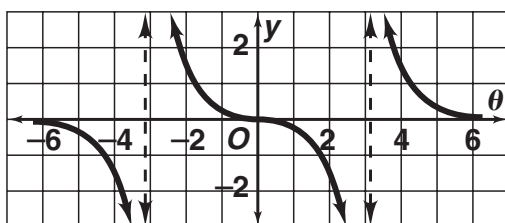
23. 6



24.  $\frac{2\pi}{5}$



25.  $\frac{2\pi^2}{3}$

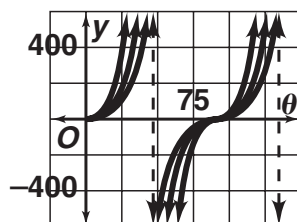


26. 1.11, 4.25

27. 2.03, 5.18

28. 0.08, 1.65, 3.22, 4.79

29. a.

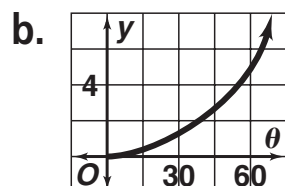


b. Check students' work; doubling the coefficient of the tangent function also doubles the output.

c. Answers may vary. Sample: the values of  $y = 600 \tan x$  will be three times greater than the values of  $y = 200 \tan x$ .

30. a.  $140.4 \text{ ft}^2$

c.  $\approx 5.2 \text{ in.}^2, \approx 15.6 \text{ in.}^2$

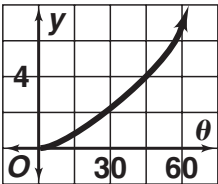
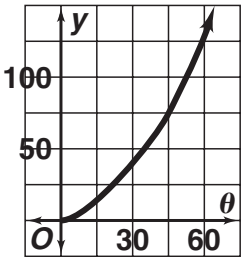


d.  $\approx 3888 \text{ tiles}, \approx 1296 \text{ tiles}$

$\approx 1.7 \text{ in.}, \approx 5.2 \text{ in.}$

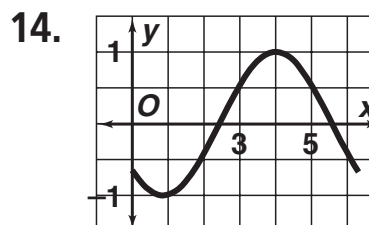
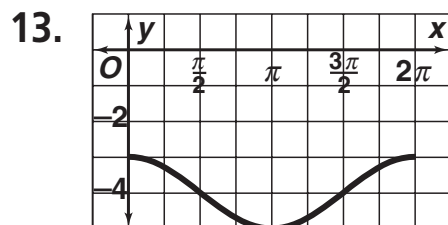
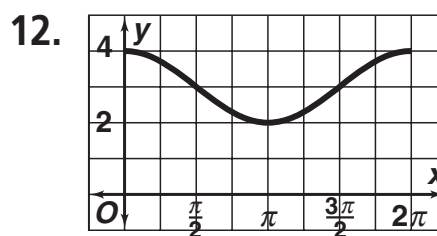
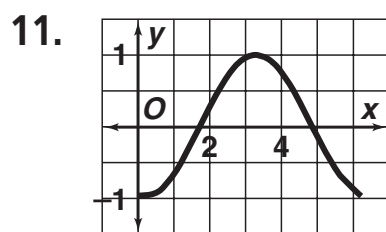
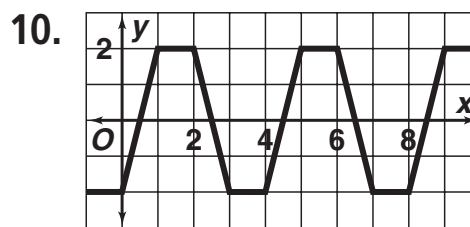
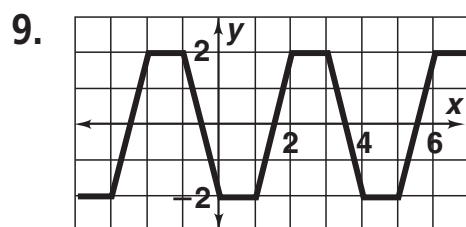
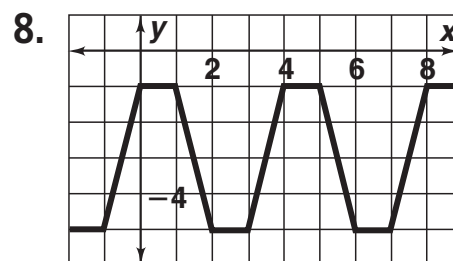
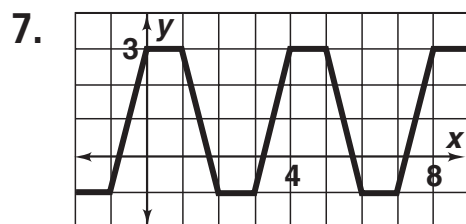
31. Check students' work.

## Answers for Lesson 13-6 Exercises (cont.)

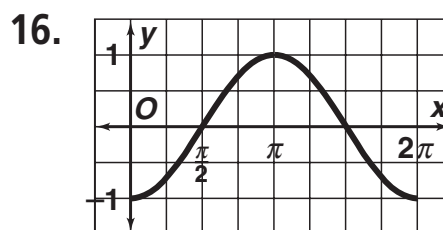
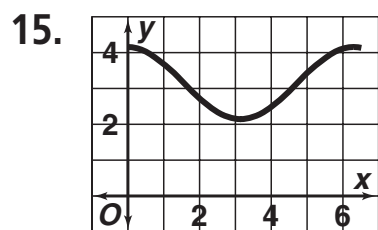
32. The asymptotes occur at  $x = -\frac{\pi}{2b}$  and  $x = \frac{\pi}{2b}$ ; adding or subtracting multiples of their difference,  $b$ , will give other asymptote values.
33. 200
34. 0
35. 135
36. -162
37. 70
38.  $y = \tan\left(\frac{1}{2}x\right)$
39.  $y = -\tan\left(\frac{1}{2}x\right)$
40.  $y = -\tan x$  or  $y = \tan(-x)$
41.  $y = \tan(2x)$
42. a.   
 $\approx 6.9$  ft
- b.  $\approx 27.7$  ft<sup>2</sup>
- c.  $\approx 166.3$  ft<sup>2</sup>
43. a.   
b.  $\approx 130$  ft
- c.  $\approx 61,500$  ft<sup>2</sup>
44. a. Check students' work.
- b. The new pattern is asymptote— $(-a)$ —zero— $(a)$ —asymptote.
45. Answers may vary. Sample: Triangles  $OAP$  and  $OBQ$  both share the angle  $\theta$  and each triangle has a right angle, so they are similar by AA.  $\frac{\sin \theta}{\cos \theta} = \frac{AP}{OA} = \frac{BQ}{OB} = \frac{\tan \theta}{1}$ . Thus  $\frac{\sin \theta}{\cos \theta} = \tan \theta$ .
46. 2; for  $0 \leq x < 2\pi$ ,  $x$  is nonnegative, and there are only 2 branches of the graph of the tangent function above the  $x$ -axis.

## Answers for Lesson 13-7 Exercises

1.  $-1$ ; 1 unit to the left
2.  $-2$ ; 2 units to the left
3.  $1.6$ ; 1.6 units to the right
4.  $3$ ; 3 units to the right
5.  $-\pi$ ;  $\pi$  units to the left
6.  $\frac{5\pi}{7}$ ;  $\frac{5\pi}{7}$  units to the right



## Answers for Lesson 13-7 Exercises (cont.)

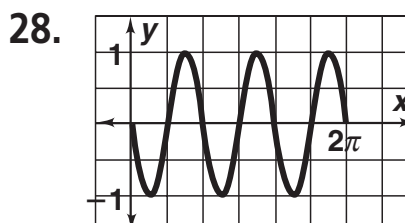
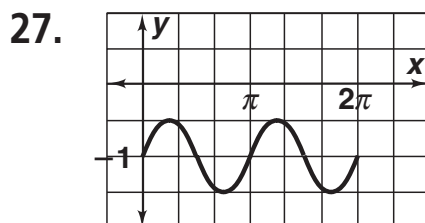
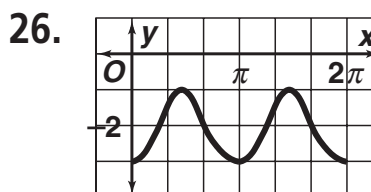
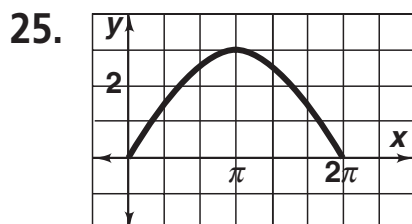
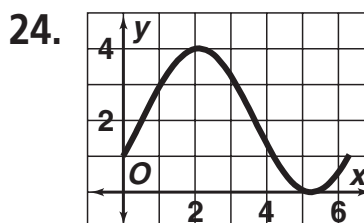
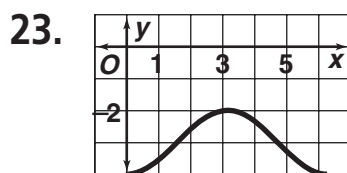
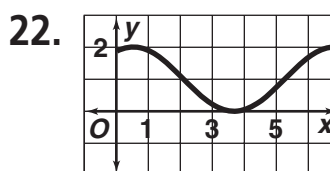
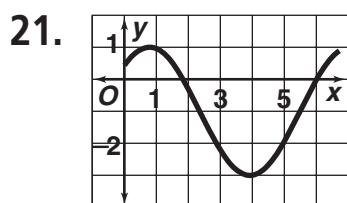


17.  $3, 2\pi$ ; 1 unit up

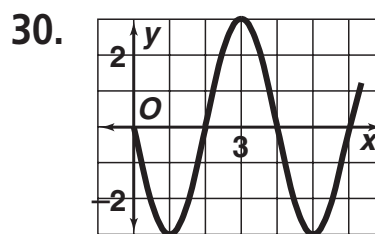
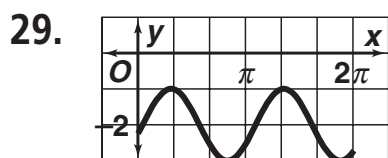
18.  $4, \pi$ ; 1 unit left and 2 units down

19.  $1, 2\pi$ ;  $\frac{\pi}{2}$  units left and 2 units up

20.  $1, 2$ ; 3 units right and 2 units up



## Answers for Lesson 13-7 Exercises (cont.)



31.  $y = \sin(x + \pi)$

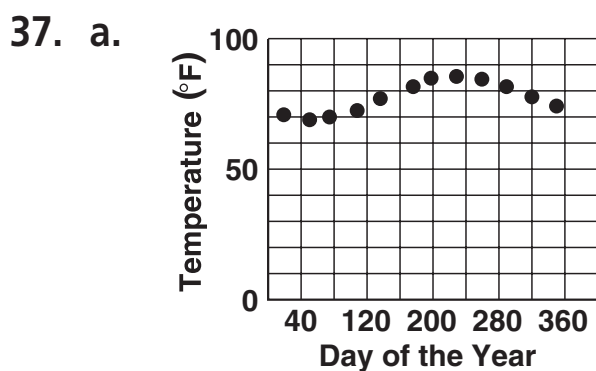
32.  $y = \cos x - \frac{\pi}{2}$

33.  $y = \sin x + 3$

34.  $y = \cos(x - 1.5)$

35.  $y = \cos\left(x + \frac{3}{2\pi}\right)$

36.  $y = \sin x - 3\pi$



b.  $y = 8.5 \cos \frac{2\pi}{365}(x - 228) + 77.5$

38.  $y = \sin(x - 2) - 4$

39.  $y = \cos(x + 3) + \pi$

40.  $y = \sin\left(x - \frac{\pi}{2}\right) + 3.5$

41.  $y = 2 \cos\left(x - \frac{\pi}{3}\right) - 1; y = 2 \sin\left(x + \frac{\pi}{6}\right) - 1$

42.  $y = -10 \cos \frac{\pi}{10}x; y = 10 \sin\left(\frac{\pi}{10}x - \frac{\pi}{2}\right)$

43. a.  $\frac{\pi}{2}; \sin x = \cos\left(x - \frac{\pi}{2}\right)$

b.  $-\frac{\pi}{2}; \cos x = \sin\left(x + \frac{\pi}{2}\right)$

44. a.  $14.5 \sin\left(\frac{2\pi}{365}(x - 105.75)\right) + 76.5$

b. The difference between the two models is the sine function is a horizontal shift of the cosine function.

c. about  $66^\circ\text{F}$

d. March 20 (day 79)



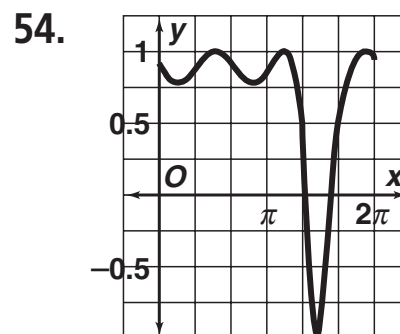
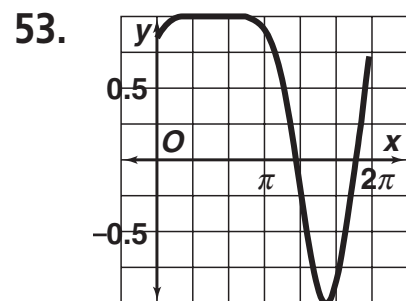
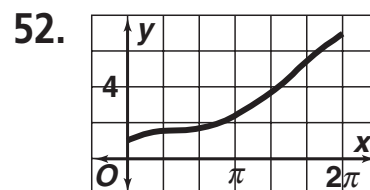
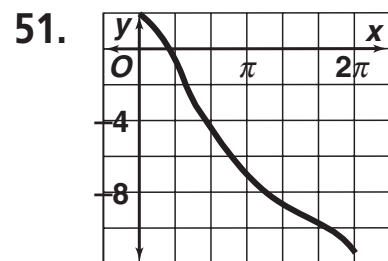
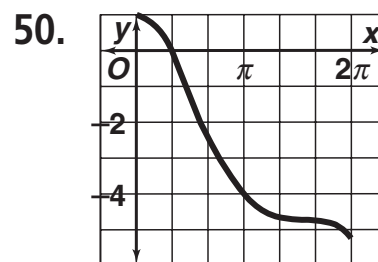
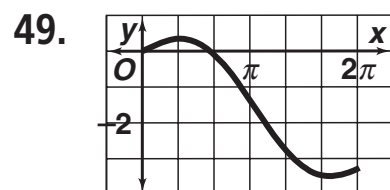
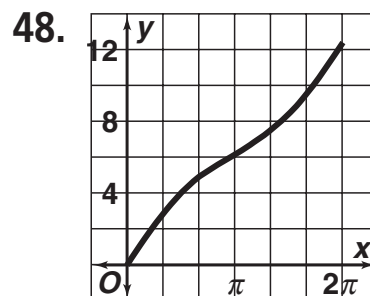
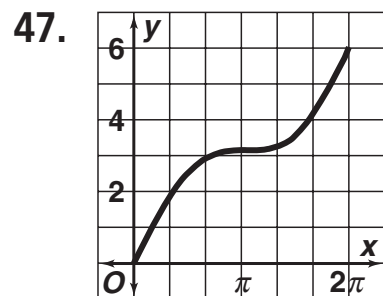
## Answers for Lesson 13-7 Exercises (cont.)

45. a. Check students' work.

b.  $g(x) = f(x + 4) - 3$

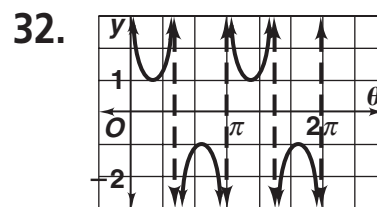
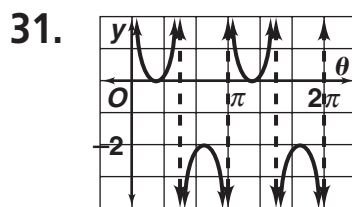
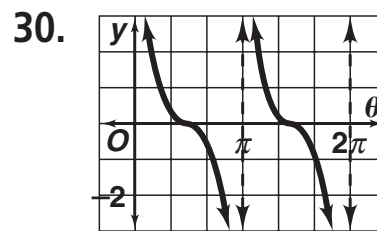
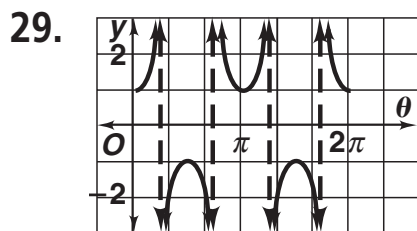
46. a.  $y = 3 \sin 2(x - 2) + 1$

b.  $3, \pi$ ; 2 units right and 1 unit up



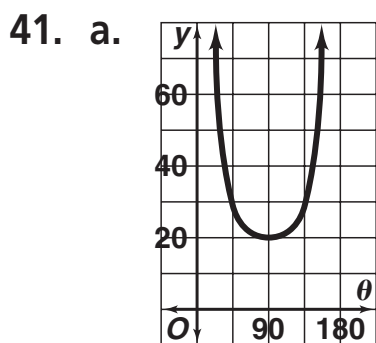
## Answers for Lesson 13-8 Exercises

- |                          |                           |                    |
|--------------------------|---------------------------|--------------------|
| 1. 1.02                  | 2. 1.02                   | 3. $-0.70$         |
| 4. $-1.06$               | 5. $\frac{3}{4}$          | 6. $\frac{18}{13}$ |
| 7. $-\frac{5}{3}$        | 8. $-\frac{3}{4}$         | 9. $\sqrt{2}$      |
| 10. $\frac{\sqrt{3}}{3}$ | 11. 0                     | 12. $-1$           |
| 13. undefined            | 14. $\frac{2\sqrt{3}}{3}$ | 15. undefined      |
| 16. $\sqrt{3}$           | 17. undefined             | 18. 2              |
| 19. 2                    | 20. $\sqrt{2}$            | 21. $-7.02$        |
| 22. $-1$                 | 23. 1                     | 24. $-1$           |
| 25. $-1.25$              | 26. 17.13                 | 27. 1.73           |
| 28. 1.02                 |                           |                    |



- |            |            |               |
|------------|------------|---------------|
| 33. 1.1547 | 34. 5.7588 | 35. $-2.9238$ |
| 36. 2      | 37. 1.0642 | 38. 1.3054    |
| 39. 1.7321 | 40. 0.5774 |               |

## Answers for Lesson 13-8 Exercises (cont.)



Note that the units on the horizontal axis are degrees.

b.  $\approx 28.3$  ft

c.  $\approx 23.1$  ft

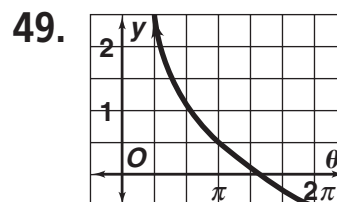
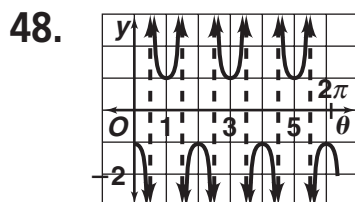
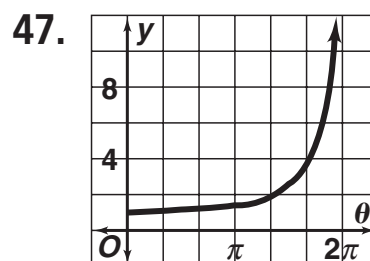
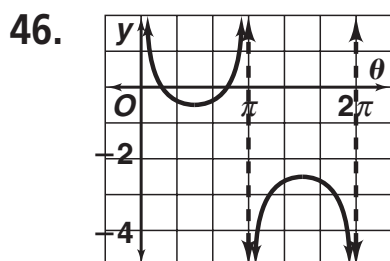
d.  $\approx 20.7$  ft

42.  $-1$

43.  $\frac{2\sqrt{3}}{3}; 1.15$

44.  $-1$

45.  $-1$



50. B

51. C

52. A

53. D

54. a. domain: all real numbers except multiples of  $\pi$ ; range: all real numbers  $\geq 1$  or  $\leq -1$ ; period  $2\pi$

b. 1

c.  $-1$

55. a. Reciprocals have the same sign.

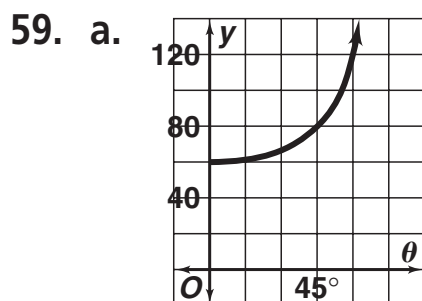
b. The reciprocal of  $-1$  is  $-1$ .

## Answers for Lesson 13-8 Exercises (cont.)

56.  $\csc 180^\circ$  is undefined because  $\sin 180^\circ$  is 0 and  $\csc \theta = \frac{1}{\sin \theta}$ .

57.  $\sec 90^\circ$  is undefined because  $\cos 90^\circ$  is 0 and  $\sec \theta = \frac{1}{\cos \theta}$ .

58.  $\cot 0^\circ$  is undefined because  $\tan 0^\circ$  is 0 and  $\cot \theta = \frac{1}{\tan \theta}$ .

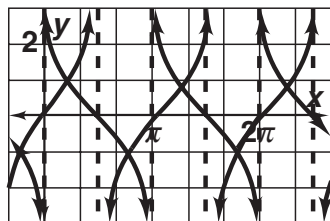


b. 63.9 ft

c. 69.3 ft

d.  $\approx 41.4^\circ$ ; 60.9 ft

60. a.

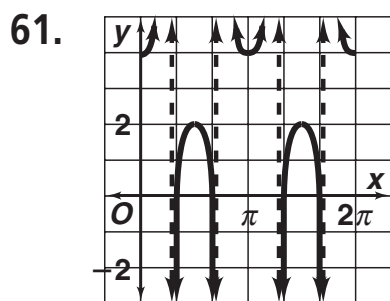


b. The domain of  $y = \tan x$  is all real numbers except odd multiples of  $\frac{\pi}{2}$ , which are its asymptotes. The domain of  $y = \cot x$  is all real numbers except multiples of  $\pi$ , which are its asymptotes. The range of both functions is all real numbers.

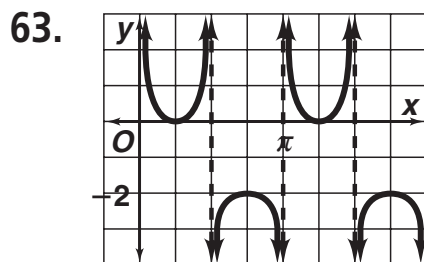
c. The graphs have the same period and range. Their asymptotes are shifted by  $\frac{\pi}{2}$ .

d. Answers may vary. Sample:  $x = \frac{\pi}{4}$ ,  $x = \frac{3\pi}{4}$

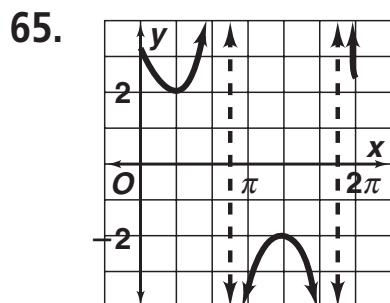
## Answers for Lesson 13-8 Exercises (cont.)



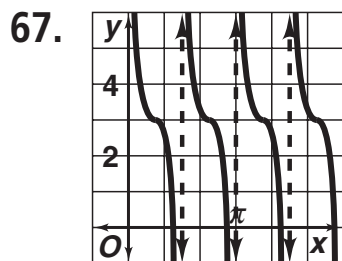
3 units up



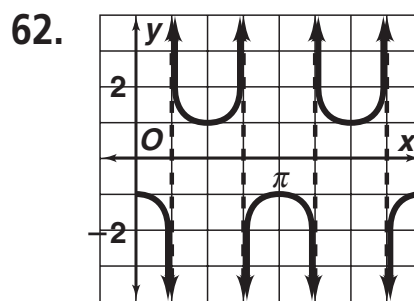
1 unit down



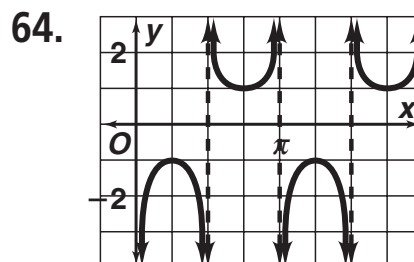
4 units right



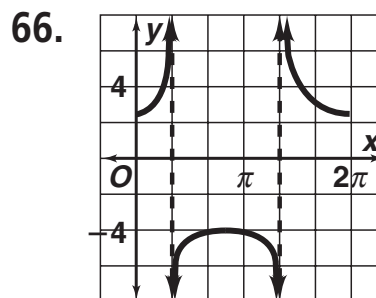
$\pi$  units left, 3 units up



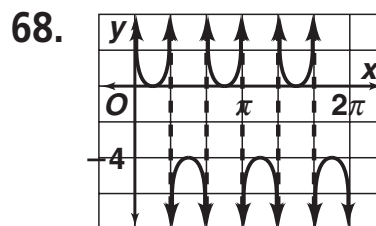
$\frac{\pi}{2}$  units left



$\frac{\pi}{2}$  units right



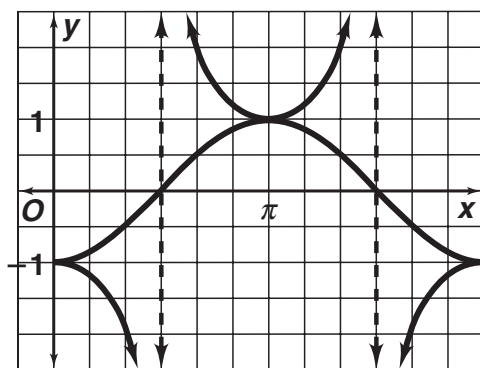
2 units left, 1 unit down



$\frac{\pi}{6}$  units right, 2 units down

## Answers for Lesson 13-8 Exercises (cont.)

69. a.



- b.  $y = -\cos x$ —domain: all real numbers; range: all real numbers between  $-1$  and  $1$ , inclusive; period:  $2\pi$ ;  
 $y = -\sec x$ —domain: all real numbers except odd multiples of  $\frac{\pi}{2}$ ; range: all real numbers except those between  $-1$  and  $1$ ; period:  $2\pi$
- c. Multiples of  $\pi$ . By definition,  $\sec x = \frac{1}{\cos x}$ , so  $-\cos x = -\sec x$  is equivalent to  $-\cos x = -\frac{1}{\cos x}$ , or  $(\cos x)^2 = 1$ . The solutions of  $(\cos x)^2 = 1$  are the values of  $x$  for which  $\cos x = 1$  or  $\cos x = -1$ . These values are the multiples of  $\pi$ .
- d. Answers may vary. Sample: The graphs have the same period and their signs are always the same. However, they have no range values in common except  $1$  and  $-1$ .
- e. The signs of  $-\sec x$  and  $-\cos x$  are the same because reciprocals have the same sign.

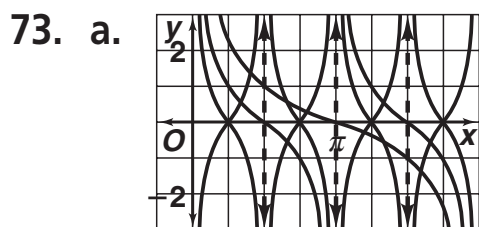
70. a. II

b. I

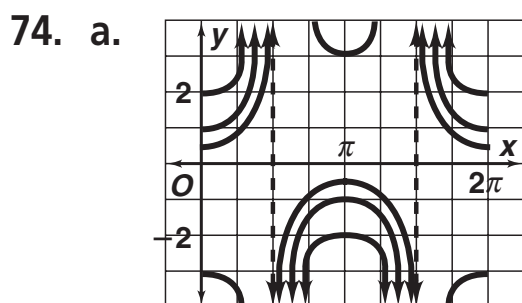
71.  $y = \sec x$  and  $y = \csc x$  are not parabolas because parabolas are not restricted by asymptotes, whereas the branches of  $y = \sec x$  and  $y = \csc x$  are between asymptotes.

72.  $y = \cos 3x$  has 3 cycles for each cycle of  $y = \cos x$ . Thus, for each cycle of  $y = \sec x$ ,  $y = \sec 3x$  has 3 cycles. Each cycle of  $y = \sec 3x$  is  $\frac{1}{3}$  as wide as one cycle of  $y = \sec x$ .

## Answers for Lesson 13-8 Exercises (cont.)



- b. Answers may vary. Sample: Given  $y = \cot bx$ , as  $|b|$  decreases, the period increases; as  $|b|$  increases, the period decreases. If  $b < 0$ ,  $y = \cot bx$  begins each branch with negative  $y$ -values and ends with positive  $y$ -values; the opposite is true for  $b > 0$ .



- b. Answers may vary. Sample: As  $|b| > 1$  increases, the graph of  $y = b \sec x$  stretches vertically away from the  $x$ -axis. As  $|b|$  decreases from 1 to 0, the graph shrinks vertically toward the  $x$ -axis. For  $b < 0$ , the graph of  $y = b \sec x$  is a reflection of  $y = |b| \sec x$  across the  $x$ -axis. The asymptotes remain the same for all values of  $b$ .