Answers for Lesson 9-1 Exercises

1.
$$y = \frac{11}{x}$$

2.
$$y = -\frac{1300}{x}$$

3.
$$y = \frac{1}{x}$$

4.
$$y = -\frac{56}{x}$$
 5. $y = \frac{3.6}{x}$

5.
$$y = \frac{3.6}{x}$$

6.
$$y = \frac{250}{x}$$

7. direct;
$$y = 5x$$

7. direct;
$$y = 5x$$
 8. inverse; $y = \frac{42}{x}$ **9.** direct; $y = 2x$

9. direct;
$$y = 2x$$

10. inverse;
$$y = \frac{0.3}{x}$$
 11. inverse; $y = \frac{1}{x}$ **12.** neither

11. inverse;
$$y = \frac{1}{x}$$

13.
$$y = \frac{100}{x}$$
; 10

14.
$$y = -\frac{80}{x}$$
; -8

13.
$$y = \frac{100}{x}$$
; 10 **14.** $y = -\frac{80}{x}$; -8 **15.** $y = -\frac{5}{3x}$; $-\frac{1}{6}$

16. A varies directly with the square of
$$r$$
.

17. A varies jointly with
$$b$$
 and h .

19.
$$V$$
 varies jointly with B and h .

20.
$$V$$
 varies jointly with h and the square of r .

21.
$$h$$
 varies directly with V and inversely with the square of r .

22. *V* varies jointly with
$$\ell$$
, w , and h .

23.
$$\ell$$
 varies directly with V and inversely with the product of w and h .

24.
$$z = \frac{5x}{y}; \frac{20}{9}$$

25.
$$z = 10xy;360$$

26.
$$z = \frac{3x^2}{y}; \frac{16}{3}$$

27.
$$z = \frac{4}{xy}; \frac{1}{9}$$

31.
$$\frac{1}{4}$$

35. 7200 rpm **36.**
$$F = k \frac{m}{d^2}$$

37.
$$18\frac{2}{3}$$

50.
$$\frac{3}{16}$$

51.
$$\frac{40}{3}$$

c.
$$d = \frac{300}{\pi r^2}$$

54. doubled; tripled

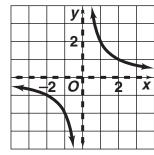
55. quartered; divided by 16

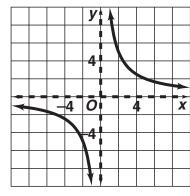
56. Division by zero is undefined.

57. $x_1y_1 = k$ and $x_2y_2 = k$ def. of inverse variation $x_1y_1 = x_2y_2$ transitivity $\frac{x_1}{x_2} = \frac{y_2}{y_1}$ Divide both sides by x_2y_1 .

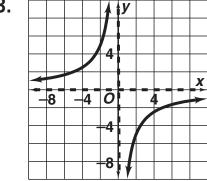
58. Answers may vary. Sample: Quadruple the volume and leave the radius constant, halve the radius and leave the volume constant, multiply the volume by 16 and double the radius, and multiply the volume and radius by $\frac{1}{4}$.

59. BMI $\approx \frac{705 \, w}{h^2}$

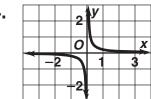




3.

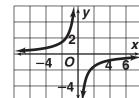


4.

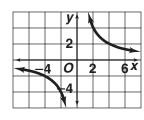


The graph is in Quadrant I and Quadrant III.

5.

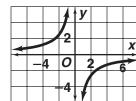


The graph is in Quadrant II and Quadrant IV. The graph is a reflection of the graph of $y = \frac{3}{x}$.



The graph is in Quadrant I and Ouadrant III.

7.



The graph is in Quadrant II and Quadrant IV. The graph is a reflection of the graph of $y = \frac{5}{x}$.

8. 10 0 10 30³ The graph is in Quadrant I and Quadrant III.

9. 0

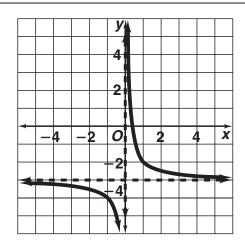
The graph is in Quadrant II and Quadrant IV. The graph is a reflection of the graph of $\frac{0.1}{x}$.

10. 18.4 ft

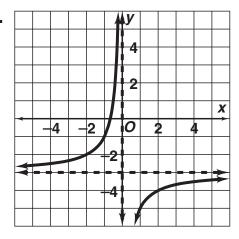
11. 7.67 ft

12. 3.83 ft

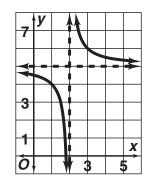
13. 1.84 ft



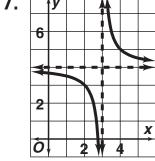
15.

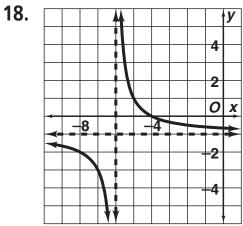


16.

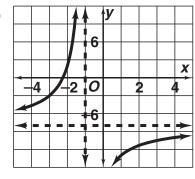


17.

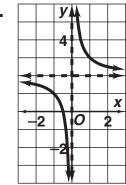


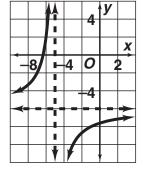


19.



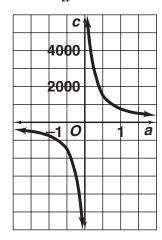
20.





24. $y = \frac{2}{x-4} - 8$

25. a. $c = \frac{750}{a}$



$$a = 0, c = 0$$

- **b.** Answers may vary. Sample: If the number of awards is large, the amount of money available for each award approaches 0. If there are a small number of awards, then the amount of money available for each award gets larger.
- 26. Check students' work.

27.
$$y = \frac{0.5}{x}$$

28.
$$y = \frac{0.75}{x}$$

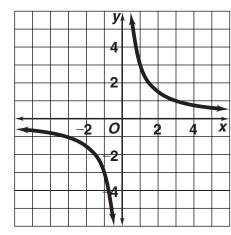
27.
$$y = \frac{0.5}{x}$$
 28. $y = \frac{0.75}{x}$ **29.** $y = \frac{-8.\overline{3}}{x}$

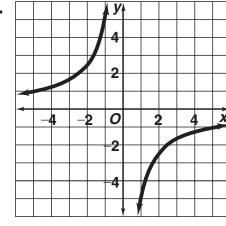
30.
$$y = \frac{-0.01}{x}$$
 31. $y = \frac{4}{x}$

31.
$$y = \frac{4}{x}$$

32.
$$y = \frac{-1.4}{x}$$

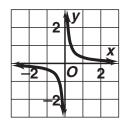
33.



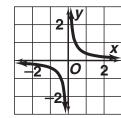


Answers for Lesson 9-2 Exercises (cont.)

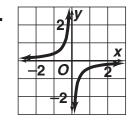
35.



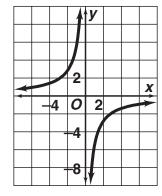
36.



37.



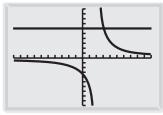
38.



- **39.** Answers may vary. Sample: The graph of the translation looks similar to the graph of $y = \frac{k}{x}$, so knowing the asymptotes helps to position the translation; check students' work.
- **40.** B

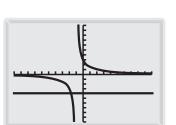
41.

43.



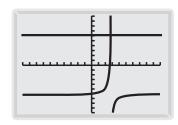
(3, 6)

(0. (



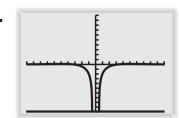
(-1.75, -4)

42.

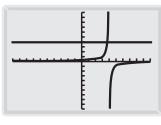


(2.92, 6.2)

44.

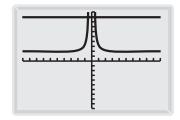


(-0.45, -10) and (0.45, -10)



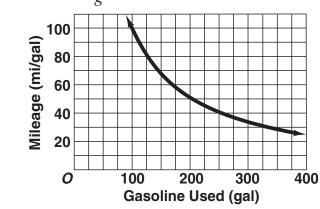
(3.76, 4.2)

46.

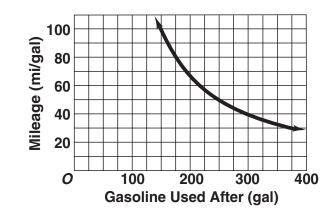


(-0.76, 9) and (0.76, 9)

47. a. $m = \frac{10,000}{g}$



b. $m = \frac{10,000}{g-50}$



c. 25 mi/gal, 28.57 mi/gal

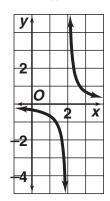
48. The branches of $y = \frac{1}{x}$ are in Quadrants I and III. The branches of $y = \left| \frac{1}{x} \right|$ are in Quadrants I and II. The graphs intersect at all points on $y = \frac{1}{x}$ in Quadrant I.

Answers for Lesson 9-2 Exercises (cont.)

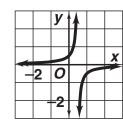
- **49.** The branches of $y = \frac{1}{x^2}$ are in Quadrants I and II. The branches of $y = \frac{1}{x}$ are in Quadrants I and III. The graphs intersect at (1, 1). The graph of $y = \frac{1}{x^2}$ is closer to the x-axis for x > 1, and the graph of $y = \frac{1}{x}$ is closer to the y-axis for 0 < x < 1.
- **50.** The branches of both graphs are in Quadrants I and II. They intersect at (1,1) and (-1,1). The graph of $y = \frac{1}{x^2}$ is closer to the x-axis for x > 1 and x < -1. The graph of $y = \left| \frac{1}{x} \right|$ is closer to the y-axis for -1 < x < 0 and 0 < x < 1.

51.
$$y = \frac{16}{x}, y = -\frac{16}{x}$$

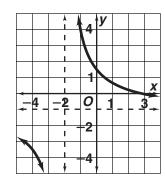
52. a.
$$y = \frac{0.\overline{6}}{x - 2}$$



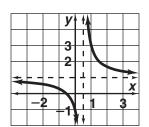
b.
$$y = \frac{-0.25}{x - 0.5}$$



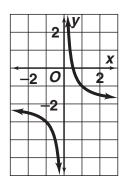
c.
$$y = \frac{5}{x+2} - 1$$



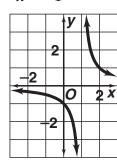
d.
$$y = \frac{2}{2x - 1} + 1$$



e. $y = \frac{1}{x} - 2$



f. $y = \frac{1}{x - 1}$



4. x = 2, x = 3 **5.** x = -3

6. $x = -\frac{7}{2}, x = 1$

7. x = 2

8. none

9. x = -2.77, x = 1.277

10. vertical asymptote at x = -2

11. hole at x = -5

12. vertical asymptotes at $x = -\frac{3}{2}$ and x = 1

13. vertical asymptote at x = -1, hole at x = 2

14. hole at x = -2

15. none

16. holes at $x = \pm 3$

17. none

18. vertical asymptote at x = -5, hole at $x = -\frac{2}{3}$

19. y = 0

20. y = 0

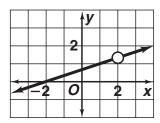
21. y = 1

22. $y = \frac{1}{2}$

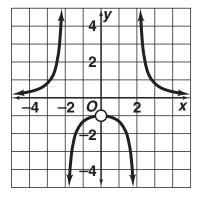
23. y = 0

24. $y = \frac{3}{4}$

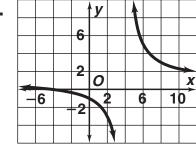
25.

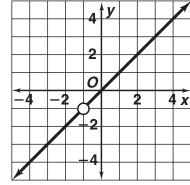


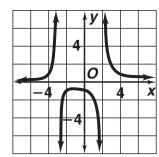
26.



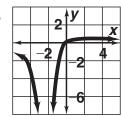
27.





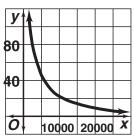


30.

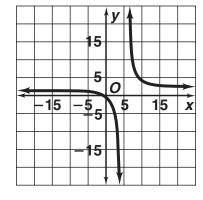


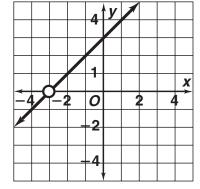
31. a.

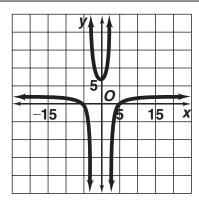
$$y = \frac{0.19x + 210,000}{x - 500}$$



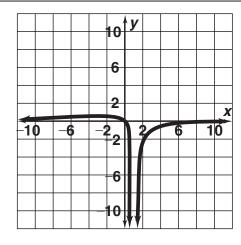
- **b.** \$46.88; \$14.68
- c. more than 21,916 discs
- **d.** x = 500, y = 0.19
- **32.** vertical asymptotes at x = -3 and x = 3, horizontal asymptote at y = 0
- **33.** vertical asymptote at x = -2
- **34.** horizontal asymptote at y = 0
- **35.**



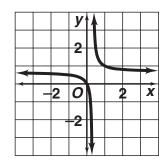




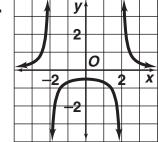
38.



39.

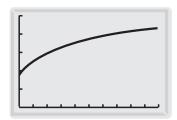


40.



41. Answers may vary. Sample: There is no value of *x* for which the denominator equals 0.

42. a.

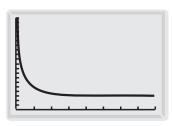


WINDOW FORMAT

Xmin=0 Xmax=100 Xscl=10 Ymin=.5 Ymax=1 Yscl=.1

b. 6 free throws

43. a. $y = \frac{20,000x + 200,000}{x + 1}$



WINDOW FORMAT

Xmin=0

Xmax=40

Xscl=4

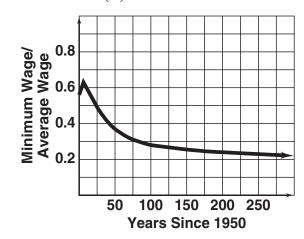
Ymin=0

Ymax=200000

Yscl=10000

- **b.** \$65,000; \$25,806.45
- **c.** Answers may vary. Sample: No; the president's salary throws off the average; the median or mode would be a better measure.
- **44.** a. $P(n) = 4n^2$
 - **b.** R(n) = 4n + 1
 - **c.** $y = \frac{4n^2}{4n+1}$; $\frac{64}{17}$ check students' work.
- **45. a.** The increase in production workers' average hourly wage is greater.
 - **b.** rational
 - $\mathbf{c.} \ \ R(x) = \frac{M(x)}{A(x)}$

d.



around the year 2106

1.
$$\frac{1}{2x-1}$$
; $x \neq 0$ or $\frac{1}{2}$

2.
$$2c + 3$$
; $c \neq 0$

3.
$$b + 1; b \neq 1$$

4.
$$z - 7$$
; $z \neq -7$

5.
$$\frac{2}{x+5}$$
; $x \neq -5$

6.
$$\frac{x+4}{x-6}$$
; $x \neq 6$ or -4

7.
$$\frac{7}{15x^2}$$
; $x \neq 0, y \neq 0$

8.
$$\frac{xy}{4}$$
; $x \neq 0$, $y \neq 0$

9.
$$\frac{4}{3}$$
; $y \neq \frac{1}{2}$ or 3

10.
$$\frac{4(x+6)}{3(3x+8)}$$
; $x \neq 3$ or $-\frac{8}{3}$

11.
$$\frac{x-2}{x(x-1)}$$
; $x \neq 0, 1, -1$, or -2 **12.** 1; $x \neq -2, -1, 2$, or 3

12.
$$1; x \neq -2, -1, 2, \text{ or } 3$$

13.
$$\frac{2}{3x^2y^2}$$
; $x \neq 0, y \neq 0$

14.
$$\frac{y}{2x^2}$$
; $x \neq 0, y \neq 0$

15.
$$\frac{5(x+y)}{3}$$
; $x \neq y$

16. 1;
$$y \neq -2$$
 or 4

17.
$$\frac{x(x-1)}{3(x+1)}$$
; $x \neq -1, 1, \text{ or } 0$ **18.** $\frac{4(y-3)}{y(y+5)}$; $y \neq 2, -5, \text{ or } 0$

18.
$$\frac{4(y-3)}{y(y+5)}$$
; $y \neq 2, -5$, or 0

19.
$$\frac{x-8}{x-10}$$
; $x \neq -3$ or 10 **20.** $\frac{y+6}{y-2}$; $y \neq 2$

20.
$$\frac{y+6}{y-2}$$
; $y \neq 2$

21.
$$\frac{y(y+3)}{12(y+4)}$$
; $x \neq 0, y \neq -4$ or 3

22.
$$\frac{6(a+1)}{a-3}$$

- 23. The student is not correct; x = 2 will make the denominator of $\frac{x}{x-2}$ equal 0, so x=2 is not a solution.
- 24. Check students' work.
- 25. The numerator and the denominator have no common factors; check students' work.

26. a.
$$\frac{\frac{2}{3}\pi r^3}{2\pi r^2 + \pi r^2} = \frac{2r}{9}$$

b.
$$\frac{\pi r^2(r)}{2\pi r^2 + 2\pi r(r)} = \frac{r}{4}$$

- c. The ratio for the cylindrical tank is larger.
- **d.** The cylindrical tank will have a larger volume.

27.
$$\frac{a+3}{(a-3)(a-3)}$$
; $a \neq -4, -3$, or 3

28.
$$\frac{2(b-5)}{b+5}$$
; $b \neq -5$

29.
$$\frac{4}{x}$$
; $x \neq 0, -5, 4$, or 1

30.
$$\frac{18x}{(x+9)(x+3)}$$
; $x \neq -9, -3, \text{ or } 3$

31.
$$\frac{x+1}{x-4}$$
; $x \neq -3, \frac{1}{2}, 2$, or 4

31.
$$\frac{x+1}{x-4}$$
; $x \neq -3, \frac{1}{2}, 2$, or 4 **32.** $\frac{x+1}{x-1}$; $x \neq -\frac{1}{2}, \frac{1}{2}, 1$, or -2

33.
$$\frac{x(x-1)^3}{(x+4)}$$
; $x \neq -4, 0, 1$ **34.** 2 ; $x \neq -3, 1$

34.
$$2; x \neq -3, 1$$

35.
$$\frac{18x^5}{y^2}$$
; $y \neq 0$

36.
$$\frac{2(a+8)}{2a+5}$$

37. a.
$$1.2 \text{ m/s}^2$$

b.
$$\approx 2.68 \text{ m/s}^2$$

38. a.
$$2x^n + 1$$

b. 2 is a factor of $2x^n$, so $2x^n$ is even, and $2x^n + 1$ is odd.

39.
$$\frac{4x}{3y}$$
; $x \neq 0$ or -1 , $y \neq 0$

39.
$$\frac{4x}{3y}$$
; $x \neq 0$ or -1 , $y \neq 0$ **40.** $-\frac{3a^2b^2}{4}$; $a \neq 0$ or $b, b \neq 0$

41.
$$\frac{15}{4n^2}$$
; $m \neq 0$ or $-\frac{2}{3}n$, $n \neq 0$

Answers for Lesson 9-5 Exercises

- 1. $\frac{120}{50} \approx 2.03$ in.
- 2. $\frac{240}{110} \approx 2.02$ in.
- **3.** For distances greater than 10 ft, d_i is nearly constant.
- **4.** 9(x + 2)(2x 1)
- **6.** $10(x-2)(x+3)^2$
- 8. 5(v + 4)(v 4)
- 10. $\frac{1}{r}$
- **12.** $\frac{xy + 8y + 4}{2xy^2}$
- **14.** $\frac{-x+6}{(x-3)(x+3)}$
- 16. $-\frac{3}{r}$
- **18.** $\frac{y-6}{2(y+2)}$
- **20.** $\frac{-5(y+8)}{(v-5)(v+5)}$
- **22.** $\frac{y}{2x}$
- **25.** $\frac{b}{0}$
- **28.** $\frac{2}{5}$
- **31.** $\frac{3x-8}{4x^2}$
- **34.** $\frac{7x-17}{(x-3)(x+3)}$ **35.** $\frac{x^2+9x-1}{(x-1)(2x+1)}$ **36.** $\frac{4x-1}{2x(2x-1)}$
- 37. $\frac{5x^2 + 6x + 12}{(x-3)(x+2)^2}$
- **39.** $\frac{4y^3 + 12y^2 y 2}{y(y + 3)}$

- 5. (x-1)(x+1)(x+1)
- 7. 18(2x 7)(x + 3)
- **9.** $2(x + 5)(x^2 32x 10)$
- **11.** $\frac{2(d-2)}{2d+1}$
- **13.** $\frac{7x^2 + 20x 18}{(x 3)(x + 3)(x + 4)}$
- **15.** $\frac{5x^2 + 14x 12}{(x 3)(x + 2)^2}$
- 17. $\frac{-3(2y+1)}{2y-1}$
- **19.** $\frac{x^2-24}{3x(x+3)}$
- **21.** $\frac{-2x(x+3)}{(x-2)(x-1)(x+1)}$
 - **24.** $\frac{2}{3(x+y)}$
- **26.** $\frac{y}{x + v}$ **27.** $\frac{3x}{2 + xy}$
- **29.** $\frac{3}{x-6}$ **30.** $\frac{-3x}{5+xy}$
- **32.** $\frac{x^2+4x-3}{(x+1)(x-1)}$ **33.** $\frac{2x^3-x^2+1}{x^2(x+1)(x-1)}$

23. $\frac{15}{28}$

- **38.** $\frac{x(3x^2+x-1)}{x^2+x^2}$
- **40.** $\frac{3(4y-21)}{y(y-7)}$
- **41.** Check students' work.

Answers for Lesson 9-5 Exercises (cont.)

- **42.** Factoring is used to determine the least common multiple of the denominators; check students' work.
- **43.** Answers may vary. Sample: Substitute 0 for x in the three expressions, and show that $\frac{4}{-9} + \frac{7}{3} \neq \frac{25}{-9}$.

44.
$$\frac{3x + 2y}{7x - 5y}$$

45.
$$\frac{2x-5y}{2(3x+2y)}$$
 46. $\frac{2(x+2)}{4x+3}$

46.
$$\frac{2(x+2)}{4x+3}$$

48.
$$\frac{2(x+5)}{x+7}$$

49.
$$\frac{-5x+13}{2(x-4)}$$

- **50.** Check students' work.
- **51.** $x \neq -2, -3, -4$; those values result in division by 0, which is undefined.

52.
$$\frac{2}{3}, \frac{3}{5}, \frac{2}{3}$$

53. a.
$$\frac{24}{7}$$
 mi/h

b.
$$\frac{24}{7}$$

c.
$$\frac{400}{9}$$
 mi/h

d.
$$\frac{2x(x+a)}{2x+a}$$
 mi/h

54. a.
$$\frac{R_1R_2R_3}{R_1R_2 + R_1R_3 + R_2R_3}$$

b.
$$\approx 0.88$$
 ohms

55. a.
$$f = \frac{d_i d_o}{d_i + d_o}$$

b.
$$\frac{x(2x+1)}{3x+1} = f$$

5. $\frac{4}{3}$ **6.** $-\frac{5}{2}$ or 4 **7.** $\frac{7}{3}$

8. 3

9. −1

10. $\frac{2}{9}$

11. 10

12. 4

13. 2

14. -1 or 2 **15.** -1 or 12 **16.** $-\frac{1}{12}$

17. about -1.45 or 1.65

18. 1

19. -3, -2

20. -9

21. 1

22. Carlos: 32 mi/h, Paul: 12 mi/h

23. passenger train: 112 mi/h, freight train: 92 mi/h

24. $2\frac{2}{3}$ h

25. $1\frac{5}{7}$ h

26. $E = \frac{mV^2}{2}$

27. $E = mc^2$

28. F = ma

29. $c = \pm \sqrt{a^2 - b^2}$

30.
$$T = \pm 2\pi\sqrt{\frac{\ell}{g}}$$

31.
$$B = \pm \frac{1}{r} \sqrt{\frac{2Vm}{q}}$$

32.
$$2\frac{2}{5}$$
 days

34. a.
$$c(x) = \frac{5.50x + 60}{x}$$

b. 14 students

35. a.
$$L = \frac{24(R-r)}{T}$$

b. 32 in., about 28.24 in., about 25.26 in.

36. a. \$1000

b.
$$\frac{15,000}{24+x}(1.60)$$

c.
$$1000 - \frac{15,000}{24 + x}(1.60)$$

d. 30 mi/gal

37. Check students' work.

40. no solution

41. no solution

44.
$$\frac{38}{21}$$

46.
$$-4$$

48.
$$-4$$

51.
$$1, -\frac{2}{3}$$

53.
$$x \approx 4.5 \text{ ft}$$

54. Check students' work.

55. a.
$$t = \frac{d}{S}$$

b.
$$\frac{35}{18}$$
 h

c.
$$\frac{d}{t} + x$$

d.
$$\frac{700}{360} + \frac{700}{360 + x} = 3.5$$
; 90 mi/h

56. a-c. Check students' work. **57.** about 44.44 mi/h

58. 5 attendants

- 1. independent
- 2. dependent
- 3. dependent

- 4. independent
- **5.** $\frac{1}{6}$

6. $\frac{9}{34}$

7. 0.54

8. $\frac{2}{x}$

- 9. $\frac{9}{25}$
- **10.** Not mutually exclusive since 2 is a prime number and less than 4.
- **11.** Mutually exclusive since if the numbers are equal, then the sum is even.
- 12. Not mutually exclusive since $6 \cdot 4 = 24$, which is greater than 20 and a multiple of 3.
- **13.** 47%

14. $\frac{3}{4}$

15. $\frac{14}{15}$

16. 39%

17. $\frac{26}{35}$

18. $\frac{1}{2}$

19. $\frac{1}{2}$

20. $\frac{5}{6}$

21. $\frac{5}{6}$

22. $\frac{2}{3}$

23. $\frac{5}{6}$

24. $\frac{5}{6}$

25. 1

26. $\frac{1}{3}$

27. $\frac{7}{12}$

28. $\frac{2}{5}$

29. $\frac{31}{56}$

- **30.** C
- **31.** 16%
- **32.** 27.6%
- **33.** 86.9%
- **34.** 37.6%

- **35.** 72.4%
- **36.** $\frac{4}{15}$
- 37. $\frac{4}{15}$
- **38.** $\frac{8}{15}$

- **39.** $\frac{1}{15}$
- **40.** $\frac{7}{15}$
- **41.** $\frac{1}{11}$
- **42.** $\frac{5}{12}$

- **43.** $\frac{7}{15}$
- **44.** $\frac{5}{2x}$

- **45.** a. $\frac{1}{4}$
 - **b.** $\frac{1}{64}$
- 46. Check students' work.
- **47.** F and G are mutually exclusive, so $P(F \text{ or } G) = P(F) + P(G) \ge 0$ and P(F and G) = 0. So $P(F \text{ or } G) \ge P(F \text{ and } G)$.
- **48.** 5%
- **49.** 6%
- **50.** 11.4%
- **51.** $\frac{4}{9}$

- **52.** a. $\frac{2}{x+2}$
 - **b.** $\frac{x-3}{2x-1}$
 - c. $\frac{2(x-3)}{(x+2)(2x-1)}$
 - **d.** $\frac{x-1}{2x-1}$