

Answers for Lesson 6-1 Exercises

1. $10x + 5$; linear binomial
2. $-3x + 5$; linear binomial
3. $2m^2 + 7m - 3$; quadratic trinomial
4. $x^4 - x^3 + x$; quartic trinomial
5. $2p^2 - p$; quadratic binomial
6. $3a^3 + 5a^2 + 1$; cubic trinomial
7. $-x^5$; quintic monomial
8. $12x^4 + 3$; quartic binomial
9. $5x^3$; cubic monomial
10. $-2x^3$; cubic monomial
11. $5x^2 + 4x + 8$; quadratic trinomial
12. $-x^4 + 3x^3$; quartic binomial
13. $y = x^3 + 1$
14. $y = 2x^3 - 12$
15. $y = 1.5x^3 + x^2 - 2x + 1$
16. $y = -3x^3 - 10x^2 + 100$
17. **a.** males: $y = -0.003357x^2 + 0.3253x + 67.05$
females: $y = -0.001929x^2 + 0.2321x + 74.89$
b. males: $y = -0.0001000x^3 + 0.002643x^2 + 0.2393x + 67.17$
females: $y = 0.0001667x^3 - 0.001193x^2 + 0.3755x + 74.69$
c. For males, the models offer similar fit. For females, the cubic model is a better fit.
18. $y = x^3 - 2x^2$; 4335
19. $y = x^3 - 10x^2$; 2023
20. $y = -0.5x^3 + 10x^2$; 433.5

Answers for Lesson 6-1 Exercises (cont.)

21. $y = -0.03948x^3 + 2.069x^2 - 17.93x + 106.9$; 206.07
22. $y = -0.007990x^3 + 0.4297x^2 - 6.009x + 43.57$; 26.34
23. $y = 0.01002x^3 - 0.3841x^2 + 5.002x + 2.132$; 25.39
24. Check students' work.
25. $x^3 + 4x$; cubic binomial
26. $-4a^4 + a^3 + a^2$; quartic trinomial
27. 7; constant monomial
28. $6x^2$; quadratic monomial
29. $x^4 + 2x^3$; quartic binomial
30. $\frac{1}{2}x^5 + \frac{2}{3}x$; quintic binomial
31. a. $V = 10\pi r^2$
b. $V = \frac{2}{3}\pi r^3$
c. $V = \frac{2}{3}\pi r^3 + 10\pi r^2$
32. Answers may vary. Sample: Cubic functions represent curvature in the data. Because of their turning points they can be unreliable for extrapolation.
33. $-c^2 + 16$; binomial
34. $-9d^3 - 13$; binomial
35. $16x^2 - x - 5$; trinomial
36. $2x^3 - 6x + 17$; trinomial
37. $a + 4b$; binomial
38. $-12y$; monomial
39. $8x^2 - 6y$; binomial
40. $-3a + 2$; binomial

Answers for Lesson 6-1 Exercises (cont.)

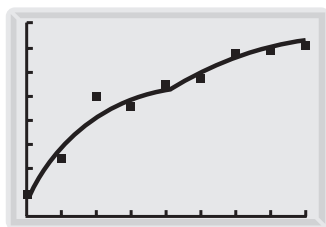
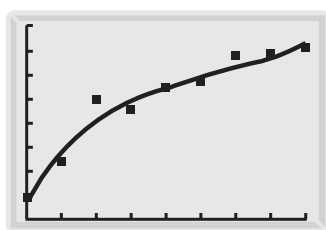
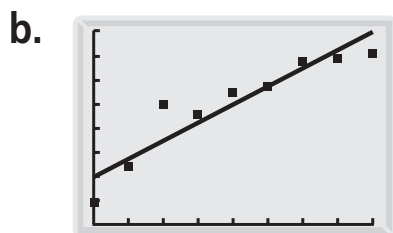
41. $2x^3 + 9x^2 + 5x + 27$; polynomial of 4 terms
42. $-4x^4 - 3x^3 + 5x - 54$; polynomial of 4 terms
43. $80x^3 - 109x^2 + 7x - 75$; polynomial of 4 terms
44. $2x^3 - 2x^2 + 8x - 27$; polynomial of 4 terms
45. $6a^2 + 3ab - 8$; trinomial
46. $8x^3 + 2x^2$; binomial
47. $30x^3 - 10x^2$; binomial
48. $2a^3 - 5a^2 - 2a + 5$; polynomial of 4 terms
49. $b^3 - 6b^2 + 9b$; trinomial
50. $x^3 - 6x^2 + 12x - 8$; polynomial of 4 terms
51. $x^4 + 2x^2 + 1$; trinomial
52. $8x^3 + 60x^2 + 150x + 126$; polynomial of 4 terms
53. $a^3 - a^2b - b^2a + b^3$; polynomial of 4 terms
54. $a^4 - 4a^3 + 6a^2 - 4a + 1$; polynomial of 5 terms
55. $12s^3 + 61s^2 + 68s - 21$; polynomial of 4 terms
56. $x^3 + 2x^2 - x - 2$; trinomial
57. $8c^3 - 26c + 12$; trinomial
58. $s^4 - 2t^2s^2 + t^4$; trinomial

Answers for Lesson 6-1 Exercises (cont.)

59. a. $y = 0.6877x + 47.97$

$$y = 0.0007125x^3 - 0.06366x^2 + 2.1690x + 41.5929$$

$$y = -0.00005632x^4 + 0.005218x^3 - 0.1757x^2 + 3.0459x + 40.7482$$



Answers may vary. Sample: The quartic model fits best.

c. For sample in part (b), 71.68×10^{15} Btu

60. $2.5 \times 10^8 \text{ cm}^3$

61. a. up 4 units

b. $y = 4x^3$ is more narrow.

c. $y = x^3$

Answers for Lesson 6-2 Exercises

1. $x^2 + x - 6$

3. $x^3 - 7x^2 + 15x - 9$

5. $x^3 + 10x^2 + 25x$

7. $x(x - 6)(x + 6)$

9. $5x(2x^2 - 2x + 3)$

11. $x(x + 4)^2$

13. about 24.2, -1.4, 0, -5, 1

15. a. $h = x$, $\ell = 16 - 2x$,

$w = 12 - 2x$

b. $V = x(16 - 2x)(12 - 2x)$

2. $x^3 + 12x^2 + 47x + 60$

4. $x^3 + 4x^2 + 4x$

6. $x^3 - x$

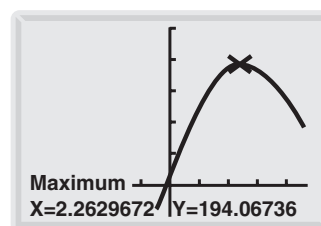
8. $3x(3x - 1)(x + 1)$

10. $x(x + 5)(x + 2)$

12. $x(x - 9)(x + 2)$

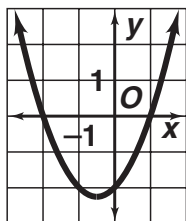
14. about 5.0, -16.9, 2, 6, 8

c.

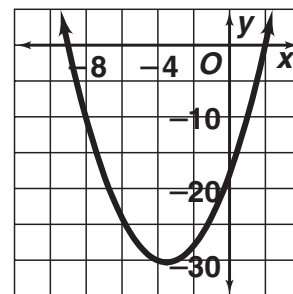


194 in.³, 2.26 in.

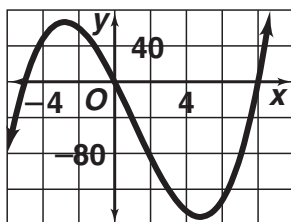
16. 1, -2



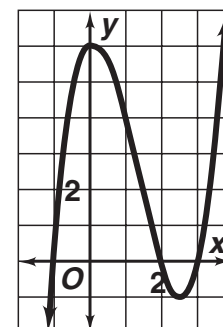
17. 2, -9



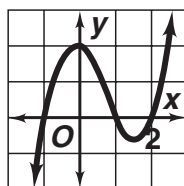
18. 0, -5, 8



19. -1, 2, 3

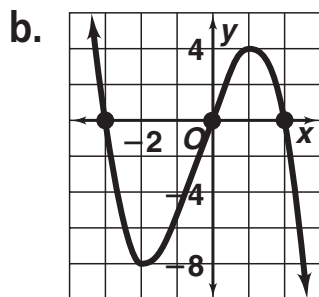


20. -1, 1, 2



Answers for Lesson 6-2 Exercises (cont.)

21. $y = x^3 - 18x^2 + 107x - 210$
22. $y = x^3 + x^2 - 2x$
23. $y = x^3 + 9x^2 + 15x - 25$ 24. $y = x^3 - 9x^2 + 27x - 27$
25. $y = x^3 + 2x^2 - x - 2$ 26. $y = x^3 + 6x^2 + 11x + 6$
27. $y = x^3 - 2x^2$ 28. $y = x^3 - \frac{7}{2}x^2 - 2x$
29. -3 (mult. 3) 30. $0, 1$ (mult. 3)
31. $-1, 0, \frac{1}{2}$ 32. $-1, 0, 1$
33. 4 (mult. 2) 34. $1, 2$ (mult. 2)
35. $-\frac{3}{2}, 1$ (mult. 2) 36. -1 (mult. 2), $1, 2$
37. $2x^3$ blocks, $15x^2$ blocks, $31x$ blocks, 12 unit blocks
38. a. $V = 2x^3 + 15x^2 + 31x + 12$; $2x^3 + 7x^2 + 7x + 2$
 b. $V = 8x^2 + 24x + 10$
39. $V = 12x^3 - 27x$
40. a. $h = x + 3$; $w = x$



$0, -3, 2$; where the volume is zero

- c. $0 < x < 2$
- d. about 4.06 ft^3
41. $y = -2x^3 + 9x^2 - x - 12$
42. $y = 5x^4 - 23x^3 - 250x^2 + 1164x + 504$

Answers for Lesson 6-2 Exercises (cont.)

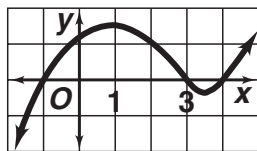
43. $y = 3x(x - 8)(x - 1)$ 44. $y = -2x(x + 5)(x - 4)$
45. $y = x^2(x + 4)(x - 1)$ 46. $y = \frac{1}{2}x\left(x - \frac{1}{2}\right)\left(x + \frac{1}{2}\right)$
47. about 10.5, -7.1 ; $\frac{3}{2}$, 4, 6
48. about 0.9, -6.9 , -1.4 ; 0, -3 , -1 , 1
49. about -2.98 , -6.17 ; 1.5 50. none, -1 ; -2 , 0
- 51–53. Answers may vary. Samples are given.**
51. $y = x^3 - 3x^2 - 10x$
52. $y = x^3 - 21x^2 + 147x - 343$
53. $y = x^4 - 4x^3 - 7x^2 + 22x + 24$
54. $-4, 5$ (mult. 3) 55. 0 (mult. 2), -1 (mult. 2) 56. 0, 6, -6
57. Answers may vary. Sample: Write the polynomial in standard form. The constant term is the value of the y -intercept.
58. 1 ft
59. Answers may vary. Sample: $y = x^4 - x^2$, and zeros are 0, ± 1 .
60. Answers may vary. Sample: The linear factors can be determined by examining the x -intercepts of the graph.
61. $x + 2a$
62. a. $A = -x^3 + 2x^2 + 4x$
b. $6\frac{7}{8}$ square units
63. Answers may vary. Sample: $y = (x - 1)(x + 1)(x - i)(x + i)$;
 $y = x^4 - 1$
64. a. Answers may vary. Sample: translation to the right 4 units
b. No; the second graph is not the result of a horizontal translation.
c. Answers may vary. Sample: rotation of 180° about the origin

Answers for Lesson 6-3 Exercises

1. $x - 8$
2. $3x - 5$
3. $x^2 + 4x + 3$, R 5
4. $2x^2 + 5x + 2$
5. $3x^2 - 7x + 2$
6. $9x - 12$, R -32
7. $x - 10$, R 40
8. $x^2 + 4x + 3$
9. no
10. yes
11. yes
12. no
13. $x^2 + 4x + 3$
14. $x^2 - 2x + 2$
15. $x^2 - 11x + 37$, R -128
16. $x^2 + 2x + 5$
17. $x^2 - x - 6$
18. $-2x^2 + 9x - 19$, R 40
19. $x + 1$, R 4
20. $3x^2 + 8x - 3$
21. $x^2 - 3x + 9$
22. $6x - 2$, R -4
23. $y = (x + 1)(x + 3)(x - 2)$
24. $y = (x + 3)(x - 4)(x - 3)$
25. $\ell = x + 3$ and $h = x$
26. 18
27. 0
28. 0
29. 12
30. 168
31. 10
32. 51
33. 0
34. $P(a) = 0$; $x - a$ is a factor of $P(x)$.
35. $x - 1$ is not a factor of $x^3 - x^2 - 2x$ because it does not divide into $x^3 - x^2 - 2x$ evenly.
36. Answers may vary. Sample: $(x^2 + x - 4) \div (x - 2)$
37. $x^2 + 4x + 5$
38. $x^3 - 3x^2 + 12x - 35$, R 109
39. $x^4 - x^3 + x^2 - x + 1$
40. $x + 4$
41. $x^3 - x^2 + 1$
42. no
43. yes
44. yes
45. no
46. no

Answers for Lesson 6-3 Exercises (cont.)

47. yes 48. yes 49. yes 50. no
51. no
52. $x^3 - x^2 + 1$
53. $x^3 - 2x^2 - 2x + 4$, R -35
54. $x^3 - 2x^2 - x + 6$
55. $x^3 - 4x^2 + x$
56. a. $x + 1$
 b. $x^2 + x + 1$
 c. $x^3 + x^2 + x + 1$
 d. $(x - 1)(x^4 + x^3 + x^2 + x + 1)$
57. a. $x^2 - x + 1$
 b. $x^4 - x^3 + x^2 - x + 1$
 c. $x^6 - x^5 + x^4 - x^3 + x^2 - x + 1$
 d. $(x + 1)(x^8 - x^7 + x^6 - x^5 + x^4 - x^3 + x^2 - x + 1)$
58. By dividing it by a polynomial of degree 1, you are reducing the degree- n polynomial by one, to $n - 1$. The remainder will be constant because it is not divisible by the variable.
59. $x + 2i$
60. Yes; the graph could rise to the right and fall to the left or it could fall to the right and rise to the left.



Answers for Lesson 6-4 Exercises (cont.)

39. $-1.04, 0, 6.04$

40. $(n - 1)(n)(n + 1) = 210; 5, 6, 7$

41. D

42. $-\frac{6}{5}, \frac{3 \pm 3i\sqrt{3}}{5}$

43. $\frac{4}{3}, \frac{-2 \pm 2i\sqrt{3}}{3}$

44. $\pm 2\sqrt{2}, \pm 2i\sqrt{2}$

45. $\pm 5, \pm i\sqrt{2}$

46. $\pm 3i, \pm i\sqrt{3}$

47. $0, \pm 2, \pm 1$

48. $\pm \sqrt{10}, \pm i\sqrt{10}$

49. $0, \frac{1}{2} \pm \frac{\sqrt{265}}{10}$

50. $4, -2 \pm 2i\sqrt{3}$

51. $0, 3 \pm \sqrt{3}$

52. $-\frac{3}{2}, 0, 4$

53. $-1, 1, \pm i\sqrt{5}$

54. $-3, -2, 2$

55. $-1, 3, 3$

56. $0, 1, 3$

57. $0, 0, 1, 6$

58. $\pm \sqrt{\frac{3}{2}}, \pm i$

59. $\pm \sqrt{2}, \pm i$

60. Check students' work.

61. $V = x^2(4x - 2)$, 4 in. by 4 in. by 16 in.

62. $x = \text{length}$, $V = x(x - 1)(x - 2)$, 5 meters

63. $-\frac{5}{2}, 1$; $y = (2x + 5)(x - 1)$

64. $\pm 3, \pm 1$; $y = (x - 1)(x + 1)(x - 3)(x + 3)$

65. $-1, 2, 2$; $y = (x + 1)(x - 2)^2$

66. $-2, 1, 3$; $y = (x + 2)(x - 1)(x - 3)$

67. $-4, -1, 3$; $y = (x + 4)(x + 1)(x - 3)$

68. A cubic can only have 3 zeros.

Answers for Lesson 6-4 Exercises (cont.)

69. a. Answers may vary. Sample: $x^4 - 9 = 0, \pm\sqrt{3}, \pm i\sqrt{3}$
b. No; two of the roots are imaginary.
70. Answers may vary. Sample: The pink block has volume $a^2(a - 3)$, the orange block has volume $9(a - 3)$, the blue block has volume $3a(a - 3)$, and the purple block has volume 27. Thus $a^3 - 27 = a^2(a - 3) + 3a(a - 3) + 9(a - 3) = (a^2 + 3a + 9)(a - 3)$.
71. a. 10
b. 8 and 12

Answers for Lesson 6-5 Exercises

1. $\pm 1, \pm 2; 1$
2. $\pm 1, \pm 2, \pm 3, \pm 6; 1, -2, -3$
3. $\pm 1, \pm 2, \pm 4; -1$
4. $\pm \frac{1}{2}, \pm 1, \pm 2, \pm 4, \pm 8; \text{no rational roots}$
5. $\pm 1, \pm 2, \pm 4, \pm 8, \pm 16; -2$
6. $\pm 1, \pm 3, \pm 5, \pm 15; \text{no rational roots}$
7. $2, \pm i\sqrt{5}$
8. $5, \pm i\sqrt{7}$
9. $-3, 1, \frac{7}{2}$
10. $-5, \frac{1 \pm \sqrt{3}}{2}$
11. $\pm \frac{1}{2}, \pm 3$
12. $1, -2, \frac{1 \pm \sqrt{7}}{3}$
13. $-\sqrt{5}, \sqrt{13}$
14. $4 + \sqrt{6}, -\sqrt{3}$
15. $1 + \sqrt{10}, 2 - \sqrt{2}$
16. $1 - i, 5i$
17. $2 - 3i, -6i$
18. $4 + i, 3 - 7i$
19. $x^3 - x^2 + 9x - 9 = 0$
20. $x^3 + 3x^2 - 8x + 10 = 0$
21. $x^3 - 2x^2 + 16x - 32 = 0$
22. $x^3 - 3x^2 - 8x + 30 = 0$
23. $x^3 - 6x^2 + 4x - 24 = 0$
24. $x^3 - x^2 + 2 = 0$
25. $\pm \frac{1}{12}, \pm \frac{1}{6}, \pm \frac{1}{4}, \pm \frac{1}{2}, \pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{3}{4}, \pm 1, \pm \frac{3}{2}, \pm 2, \pm 3, \pm 6; \frac{1}{2}, \frac{3}{2}, \frac{2}{3}$
26. $\pm \frac{1}{10}, \pm \frac{1}{5}, \pm \frac{2}{5}, \pm \frac{1}{2}, \pm \frac{4}{5}, \pm 1, \pm 2, \pm \frac{5}{2}, \pm 4, \pm 5, \pm 10, \pm 20; 2, \frac{2}{5}, \frac{5}{2}$
27. $\pm \frac{7}{3}, \pm \frac{1}{6}, \pm \frac{1}{2}, \pm \frac{1}{3}, \pm \frac{7}{6}, \pm 1, \pm \frac{3}{2}, \pm 3, \pm \frac{7}{2}, \pm 7, \pm \frac{21}{2}, \pm 21; \frac{1}{3}, -\frac{7}{2}, 1, 3$
28. $\pm \frac{1}{4}, \pm \frac{5}{4}, \pm \frac{1}{2}, \pm \frac{3}{4}, \pm \frac{1}{8}, \pm \frac{5}{8}, \pm \frac{3}{8}, \pm \frac{15}{4}, \pm \frac{5}{2}, \pm 1, \pm \frac{3}{2}, \pm \frac{15}{8}, \pm \frac{15}{2}, \pm 15, \pm 3, \pm 5; -\frac{1}{2}, \frac{3}{2}, \frac{5}{2}$
29. $x^4 - 6x^3 + 14x^2 - 24x + 40 = 0$
30. $x^4 - 2x^3 - x^2 + 6x - 6 = 0$
31. $x^4 - 6x^3 + 2x^2 + 30x - 35 = 0$

Answers for Lesson 6-5 Exercises (cont.)

32. Never true; 5 is not a factor of 8, so by the Rational Root Theorem, 5 is not a root of the equation.
33. Sometimes true; since -2 is a factor of 8, -2 is a possible root of the equation.
34. Always true; use the Rational Root Theorem with $p = a$ and $q = 1$.
35. Sometimes true; since $\sqrt{5}$ and $-\sqrt{5}$ are conjugates, they can be roots of a polynomial equation with integer coefficients.
36. Never true; since $2 + i$ and $-2 - i$ are not conjugates, they cannot be the only imaginary roots of a polynomial equation with integer roots. If their conjugates were also roots, there would be four roots and the equation would have to be of fourth degree.
37. D
38. If $2i$ is a root, then so is $-2i$.
39. Answers may vary. Sample: $x^4 - x^2 - 2 = 0$; roots are $\pm\sqrt{2}$ and $\pm i$.
40. a. 2 real, 2 imaginary; 4 imaginary; 4 real
b. 5 real; 3 real, 2 imaginary; 4 imaginary, 1 real
c. Answers may vary. Sample: It has an odd number of real solutions, but it must have at least one real solution.
41. Answers may vary. Sample: You cannot use the Irrational Root Theorem unless the equation has rational coefficients.
42. $x^2 + (-2 + i)x + 12 - 8i = 0$
43. a-c. Answers may vary. Sample:
a. $x - 1 - \sqrt{2} = 0$
b. $x^2 - 2(1 + \sqrt{2})x + (1 + \sqrt{2})^2 = 0$
c. -1

Answers for Lesson 6-6 Exercises

- 3 complex roots; number of real roots: 1 or 3
possible rational roots: ± 1
- 2 complex roots; number of real roots: 0 or 2
possible rational roots: $\pm \frac{1}{3}, \pm \frac{7}{3}, \pm 1, \pm 7$
- 4 complex roots; number of real roots: 0, 2, or 4
possible rational roots: 0
- 5 complex roots; number of real roots: 1, 3, or 5
possible rational roots: $\pm \frac{1}{2}, \pm 1, \pm \frac{5}{2}, \pm 5$
- 7 complex roots; number of real roots: 1, 3, 5, or 7
possible rational roots: $\pm 1, \pm 3$
- 1 complex root number of real roots: 1
possible rational roots: $\pm \frac{1}{4}, \pm \frac{1}{2}, \pm 1, \pm 2, \pm 4, \pm 8$
- 6 complex roots; number of real roots: 0, 2, 4, or 6
possible rational roots: $\pm \frac{1}{2}, \pm 1, \pm \frac{7}{2}, \pm 7$
- 10 complex roots; number of real roots: 0, 2, 4, 6, 8, or 10
possible rational roots: ± 1
- $-1, \frac{1 \pm i\sqrt{7}}{4}$
- $4, \frac{1 \pm i\sqrt{3}}{2}$
- $\pm 2, \pm \sqrt{2}$
- $0, \frac{3 \pm 3\sqrt{5}}{2}$
- 3, $\pm i$
- $2, \pm \sqrt{3}$
- $\pm 2, \pm i$
- $-6, \pm i$
- 4 complex roots; number of real roots: 0, 2, or 4
possible rational roots: $\pm \frac{1}{2}, \pm 1, \pm 2, \pm \frac{13}{2}, \pm 13, \pm 26$
- 5 complex roots; number of real roots: 1, 3, or 5
possible rational roots: $\pm 1, \pm 2, \pm 3, \pm 6, \pm 9, \pm 18$
- 3 complex roots; number of real roots: 1 or 3
possible rational roots: $\pm \frac{1}{3}, \pm \frac{2}{3}, \pm 1, \pm \frac{4}{3}, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12$

Answers for Lesson 6-6 Exercises (cont.)

20. 6 complex roots; number of real roots: 0, 2, 4, or 6
possible rational roots: $\pm\frac{1}{4}, \pm\frac{1}{2}, \pm\frac{3}{4}, \pm 1, \pm\frac{3}{2}, \pm 2, \pm 3, \pm 4, \pm 6, \pm 8, \pm 12, \pm 24$

21. $4, \pm 3i$

22. $-2, \pm\sqrt{5}$

23. $-6, \frac{-1 \pm i}{2}$

24. $-\frac{1}{4}, -1 \pm 2i$

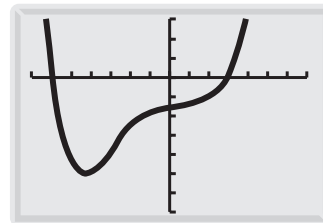
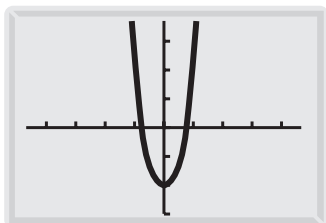
25. $\frac{1}{2}, \pm 2i\sqrt{5}$

26. $\frac{2}{5}, \frac{-1 \pm i\sqrt{11}}{6}$

27. Answers may vary. Sample: $y = x^4 + 3x^2 + 2$

28. ± 0.75

29. $-3.24, 1.24$



30. If you have no constant, then all terms have an x that can be factored out. The resulting expression will have a constant that can be used in the Rational Root Theorem.

31. Yes; for example, $2x^2 - 11x + 5 = 0$ has roots 0.5 and 5.

Answers for Lesson 6-7 Exercises

- 1. 120
- 2. 3,628,800
- 3. 6,227,020,800
- 4. 720
- 5. 665,280
- 6. 120
- 7. 120
- 8. 3003
- 9. a. 24
b. 120
- 10. 8
- 11. 56
- 12. 336
- 13. 1680
- 14. 6
- 15. 120
- 16. 60,480
- 17. 60
- 18. 10,897,286,400
- 19. 4,151,347,200
- 20. 12
- 21. 15
- 22. 56
- 23. 1
- 24. 4
- 25. 35
- 26. 15
- 27. 35
- 28. $\frac{5}{18}$
- 29. 4368
- 30. 21
- 31. 2600
- 32. 126
- 33. true because of the Comm. Prop. of Add.
- 34. true because of the Assoc. Prop. of Mult.
- 35. False; answers may vary. Sample: $(3 + 2)! = 120$ and $3! + 2! = 8$
- 36. False; answers may vary. Sample: $(3 \times 2)! = 720$ and $3! \times 2! = 12$
- 37. False; answers may vary. Sample: $(3!)! = 720$ and $(3!)^2 = 36$
- 38. False; answers may vary. Sample: $(3!)^2 = 36$ and $3^{(2!)} = 9$
- 39. C
- 40. 60
- 41. 2 ways, because order matters

Answers for Lesson 6-7 Exercises (cont.)

42. $\frac{4}{19,393} \approx .000206$ 43. 84 44. $\frac{12}{49}$
45. 5 46. permutation 47. permutation
48. combination 49. combination 50. 330,791,175
51. 210 52. 12,650 53. 5 54. 9504
55. a. 56
b. 56
c. Answers may vary. Sample: Each time you choose 3 of the 8 points to use as vertices of a \triangle , the 5 remaining points could be used to form a pentagon.
56. 120 57. 3024 58. 360 59. 24
60. 1680 61. 840 62. 5040 63. 0
- 64–67. Check students' work.**
68. a. 2048
b. Answers may vary. Sample: No, because there are too many possible solutions.
69. a. The graph for $y = {}_x C_{x-2}$ is identical to the graph for $y = {}_x C_2$ because ${}_2 C_{2-2} = {}_2 C_2$, ${}_3 C_{3-2} = {}_3 C_2$, ${}_4 C_{4-2} = {}_4 C_2$, ${}_5 C_{5-2} = {}_5 C_2$, etc.
b. Answers may vary. Sample: The function is defined only at discrete whole-number values of x , and not over a smooth range of points as in a continuous function.
70. a. 35
b. 6
c. ${}_7 C_3 = \frac{7!}{3!4!}$, so ${}_7 C_3 \cdot 3! = \frac{7!}{4!}$, which is the permutation formula for ${}_7 P_3$.

Answers for Lesson 6-7 Exercises (cont.)

71. a. All the terms contain the factors 2 and 5. Since multiplication is commutative, $2 \times 5 = 10$ and 10 times any integer ends in zero.
b. 24 zeros
72. Answers may vary. Sample: 99
73. a. 18 people
b. 8568
c. 658,008
d. about 0.013 or 1.3%

Answers for Lesson 6-8 Exercises

1. $a^3 + 3a^2b + 3ab^2 + b^3$
2. $x^2 - 2xy + y^2$
3. $a^4 + 4a^3b + 6a^2b^2 + 4ab^3 + b^4$
4. $x^5 - 5x^4y + 10x^3y^2 - 10x^2y^3 + 5xy^4 - y^5$
5. $a^6 - 6a^5b + 15a^4b^2 - 20a^3b^3 + 15a^2b^4 - 6ab^5 + b^6$
6. $x^7 - 7x^6y + 21x^5y^2 - 35x^4y^3 + 35x^3y^4 - 21x^2y^5 + 7xy^6 - y^7$
7. $x^8 + 8x^7y + 28x^6y^2 + 56x^5y^3 + 70x^4y^4 + 56x^3y^5 + 28x^2y^6 + 8xy^7 + y^8$
8. $d^9 + 9d^8 + 36d^7 + 84d^6 + 126d^5 + 126d^4 + 84d^3 + 36d^2 + 9d + 1$
9. $x^3 - 9x^2 + 27x - 27$
10. $a^4 + 12a^3b + 54a^2b^2 + 108ab^3 + 81b^4$
11. $x^6 - 12x^5 + 60x^4 - 160x^3 + 240x^2 - 192x + 64$
12. $x^8 - 32x^7 + 448x^6 - 3584x^5 + 17,920x^4 - 57,344x^3 + 114,688x^2 - 131,072x + 65,536$
13. $x^4 + 4x^3y + 6x^2y^2 + 4xy^3 + y^4$
14. $w^5 + 5w^4 + 10w^3 + 10w^2 + 5w + 1$
15. $s^2 - 2st + t^2$
16. $x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1$
17. $x^4 - 4x^3y + 6x^2y^2 - 4xy^3 + y^4$
18. $p^7 + 7p^6q + 21p^5q^2 + 35p^4q^3 + 35p^3q^4 + 21p^2q^5 + 7pq^6 + q^7$
19. $x^5 - 15x^4 + 90x^3 - 270x^2 + 405x - 243$
20. $64 - 48x + 12x^2 - x^3$

Answers for Lesson 6-8 Exercises (cont.)

21. a. about 25%

b. about 21%

c. about 12%

22. about 66%

23. $x^7 + 7x^6y + 21x^5y^2 + 35x^4y^3 + 35x^3y^4 + 21x^2y^5 + 7xy^6 + y^7$

24. $x^8 - 40x^7y + 700x^6y^2 - 7000x^5y^3 + 43,750x^4y^4 - 175,000x^3y^5 + 437,500x^2y^6 - 625,000xy^7 + 390,625y^8$

25. $81x^4 - 108x^3y + 54x^2y^2 - 12xy^3 + y^4$

26. $x^5 - 20x^4y + 160x^3y^2 - 640x^2y^3 + 1280xy^4 - 1024y^5$

27. $117,649 - 201,684x + 144,060x^2 - 54,880x^3 + 11,760x^4 - 1344x^5 + 64x^6$

28. $8x^3 + 36x^2y + 54xy^2 + 27y^3$

29. $x^4 + 2x^2y^2 + y^4$

30. $x^6 - 6x^4y + 12x^2y^2 - 8y^3$

31. $x^6 + 6x^5 + 15x^4 + 20x^3 + 15x^2 + 6x + 1$

32. $x^6 - 6x^5 + 15x^4 - 20x^3 + 15x^2 - 6x + 1$

33. $x^5 + 10x^4 + 40x^3 + 80x^2 + 80x + 32$

34. $x^5 - 10x^4 + 40x^3 - 80x^2 + 80x - 32$

35. $16x^4 + 96x^3y + 216x^2y^2 + 216xy^3 + 81y^4$

36. $27x^3 + 135x^2y + 225xy^2 + 125y^3$

37. $64x^6 - 384x^5y + 960x^4y^2 - 1280x^3y^3 + 960x^2y^4 - 384xy^5 + 64y^6$

38. $81x^4 + 216x^3y + 216x^2y^2 + 96xy^3 + 16y^4$

39. $32x^5 + 80x^4y + 80x^3y^2 + 40x^2y^3 + 10xy^4 + y^5$

Answers for Lesson 6-8 Exercises (cont.)

40. $2187x^7 + 5103x^6y + 5103x^5y^2 + 2835x^4y^3 + 945x^3y^4 + 189x^2y^5 + 21xy^6 + y^7$
41. $x^6 - 18x^5y + 135x^4y^2 - 540x^3y^3 + 1215x^2y^4 - 1458xy^5 + 729y^6$
42. $x^3 + 15x^2y + 75xy^2 + 125y^3$
43. a. about 31%
b. about 16%
c. about 16%
44. a. 6
b. 84
45. ${}_8C_4x^4y^4$
46. 9
47. $7, 7r^6s$
48. $594x^{10}$
49. $80x^2$
50. $27x^8$
51. $264x^{10}$
52. x^{11}
53. $64y^6$
54. $-823,680x^8y^7$
55. $314,928x^7$
56. $29,568x^{10}y^6$
57. $1716x^{12}y^{14}$
58. Answers may vary. Sample: Since one of the terms is negative and it is alternately raised to odd and even powers, the term is negative when raised to an odd power and positive when raised to an even power.
59. a. $(s + 0.5)^3$
b. $s^3 + 1.5s^2 + 0.75s + 0.125$
60. The exponent of q should be 5 because the exponent of q should be the degree (7) minus the exponent of p .

Answers for Lesson 6-8 Exercises (cont.)

61. $13, d^{12}, 12d^{11}e$

62. $16, x^{15}, -15x^{14}y$

63. $6, 32a^5, 80a^4b$

64. $8, x^7, -21x^6y$

65. a. -4

b. $(1 - i)^4 = 1 - 4i - 6 + 4i + 1 = -4 \quad \checkmark$

66. $(-1 + \sqrt{3} \cdot i)^3 = -1 + 3i\sqrt{3} + 9 - 3i\sqrt{3} = 8 \quad \checkmark$

67. Answers may vary. Sample: A coin is tossed five times with the probability of heads on each toss 0.5. Write an expression for the probability of exactly 2 heads being tossed.

68. a. $(k + 1)! = (k + 1) \cdot (k) \cdot (k - 1) \cdot \dots \cdot 1 = (k + 1)[(k) \cdot (k - 1) \cdot \dots \cdot 1] = (k + 1) \cdot k!$

b. The derivation below finds a common denominator for the fractions that represent ${}_nC_k$ and ${}_nC_{k+1}$, and then uses algebra to show that ${}_nC_k + {}_nC_{k+1} = {}_{n+1}C_{k+1}$. In addition, the identity from part (a) is used three times.

$$\begin{aligned} {}_nC_k + {}_nC_{k+1} &= \frac{n!}{k!(n-k)!} + \frac{n!}{(k+1)!(n-k-1)!} = \\ &= \frac{(k+1)n!}{(k+1)!(n-k)!} + \frac{(n-k)n!}{(k+1)!(n-k)!} = \\ &= \frac{(k+1+n-k)n!}{(k+1)!(n-k)!} = \frac{(n+1)n!}{(k+1)!(n-k)!} = \\ &= \frac{(n+1)!}{(k+1)!((n+1)-(k+1))!} = {}_{n+1}C_{k+1} \end{aligned}$$

c. If you consider the row of Pascal's Triangle containing just 1 to be row zero, ${}_4C_2$ is 6, the third entry in the fourth row. ${}_4C_3$ is 4, the fourth entry in the fourth row. ${}_5C_3$ is 10, the fourth entry in the fifth row.
 ${}_4C_2 + {}_4C_3 = 6 + 4 = 10 = {}_5C_3$