

## Warm Up

State the percent of increase or decrease of each:

1)  $y = 6(1.12)^x$       2)  $y = 5(0.67)^x$

$\uparrow 1.12 - 1 = .12 \rightarrow 12\%$      
  $\downarrow .67 - 1 = -.33 \rightarrow 33\%$



3) The student enrollment at EHS in 1990 was 720 and increased 2.6% each year up until now. If the rate continues at 2.6% per year, what is the expected student enrollment for 2020.

$$y = ab^x$$

$$b = 1 + r$$

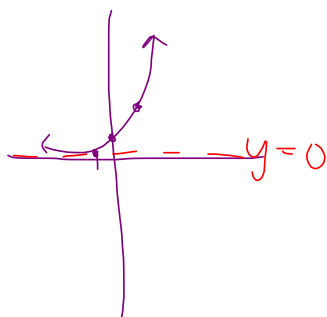
$$y = 720(1.026)^{30}$$

Graph the following, without a calculator:

→ 4)  $y = 3^x$

Without a calculator, try to graph  $y = 3^x + 4$

X	y
-1	1/3
0	1
1	3



20  $\log_5(-25)$

↑

$$5^x = -25$$

$$5^{-5} = \frac{1}{5^5}$$

x	y
-1	
0	
1	

$$5^x$$

x	y
	-1
	0
	1

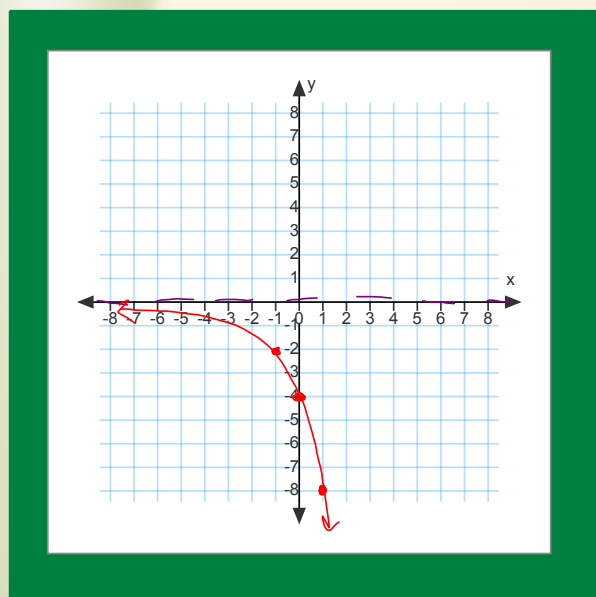
$$\log_5 x$$

## 8.2 Properties of Exponential Functions

Let's graph  $y = -4(2)^x$

x	y
-1	-2
0	-4
1	-8

Do you remember...



$$D: (-\infty, \infty)$$

$$R: (-\infty, 0)$$

expon.

$$y = 3(2)^x$$

$$D: (-\infty, \infty)$$

logs

$$y = \log_5 x$$

$$D: (0, \infty)$$

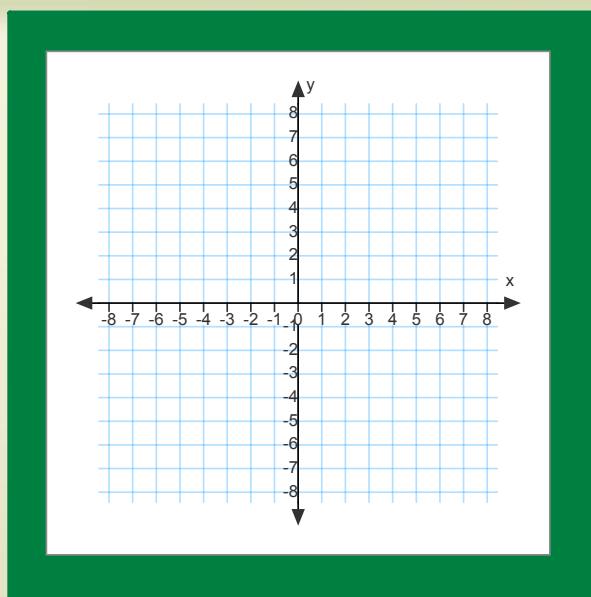
Translating  $y = ab^x$ 

$y = ab^{x-h}$   
is a horizontal shift

$-h$        $+h$   
Right      left

$y = ab^x + k$   
is a vertical shift

$+k$        $-k$   
up      down



$$y = 2(3)^x$$

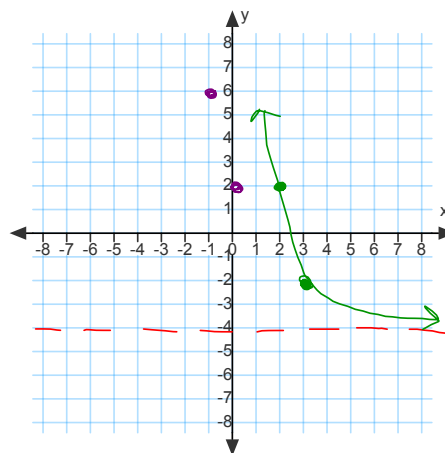
left 4  
up 2

Graph the stretch first of  $y = 6\left(\frac{1}{3}\right)^x$   
 then graph  $y = 6\left(\frac{1}{3}\right)^{x-3} - 4$

①  $y = 6\left(\frac{1}{3}\right)^x$

x	y
-1	18
0	6
1	2

② Right 3  
 Down 4

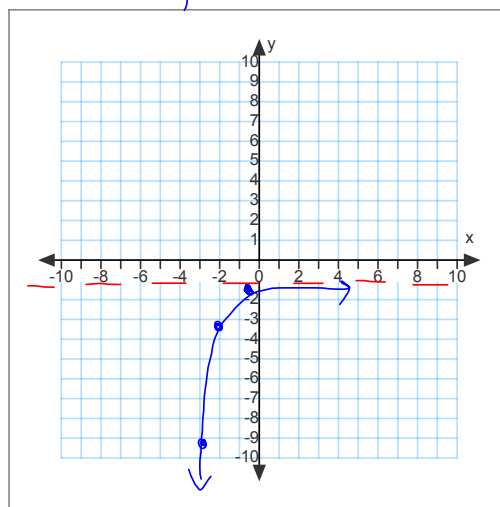


$y = -2\left(\frac{1}{4}\right)^{x+2} - 1$

$-2 \cdot \frac{1}{4} \left(\frac{1}{4}\right)^1$

x	y
-1	-8
0	-2
1	-1/2

$\left(\frac{1}{4}\right)^{-1} = 4$



## The number $e$



$$e \approx 2.7$$

Exponential functions with a base of  $e$  are useful for describing continuous growth or decay.

Use the graph of  $y = e^x$  to evaluate the expression to four decimal places.

$$y = e^0 \quad e^1$$

$$e^3 = 20.0855$$

To calculate continuously compounded interest use the formula below.  
In the formula,  $A$  represents the amount in the account

**Amount**

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$$A = Pe^{rt}$$

Ending  
Amount

Initial  
Amount

Rate  
(decimal)

time  
(years)

## Continuously Compounded Interest Formula

\$500

compounded continuously  
@ 3.7% → 10 years?

$$A = Pe^{rt}$$

### What in real life is ever continuously compounded?

**Nature doesn't wait for a human year before changing** Interest earnings are a type of "growth", but natural phenomena like temperature and radioactive decay change constantly, every second and faster. This is one reason why science equations model change with "e" and not " $(1+r/n)^n$ ":

Nature rudely ignores our calendar when making adjustments.



Without graphing, determine whether each equation represents exponential growth or exponential decay.

$$e \approx 2.7$$

$$f(x) = 3e^x$$

$$y = -4\left(\frac{e}{2}\right)^x$$

$$f(x) = \left(\frac{1}{e}\right)^x$$

Growth

Growth

Decay

Erase to reveal the answers!

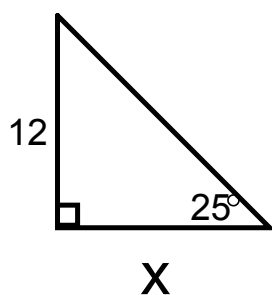
## HOMework 8.2

p. 442 #1-11 odd, 19-23  
odd, 24-26 all, 30, 36,  
42-47 all, 51-53 all

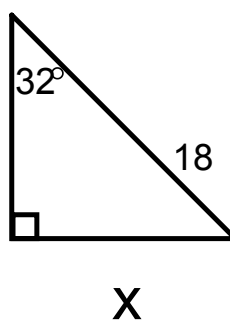


Use your calculator and SOHCAHTOA to find the following.

1.



2.



3.

